

Qucs

Reference Manual Measurement Expressions Reference Manual

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Introduction

This manual describes the measurement expressions available in "Qucs", the "Quite Universal Circuit Simulator".

Measurement expressions come into play whenever the results of a "Qucs" simulation run need post processing. Examples would be the conversion of a simulated voltage waveform from volts to dBV, the root mean square value of that waveform or the determination of the peak voltage. The "Qucs" measurement functions offer a rich set of data manipulation tools.

If you are not familiar with the way how to enter those formulas, please refer to chapter "*Using Measurement Expressions*", which points out the possibilities to create and change measurement expressions. Also the data types supported are specified here. Chapter "*Functions Syntax and Overview*" introduces the basic syntax of functions and a categorical list of all functions available. The core of the document, a detailed compilation of all "Qucs" functions divided into different categories, is presented in chapter "*Math Functions*" and chapter "*Electronics Functions*". Finally, the *Index* contains an alphabetical list of all functions.

Using Measurement Expressions

The chapter describes the usage of mathematical expressions for post processing simulation data in "Qucs", how to enter formulas and modifying them. It gives a brief description of the overall syntax of those expressions.

Entering Measurement Expressions

Measurement expressions generate new datasets by function or operator driven evaluation of simulation results. Those new datasets are accessible in the data display tab after simulation. The related equations can be entered into the schematic editor by the following means:

- Using the equation icon in the "Tools" bar (see fig. 1)
- Using menu item "Insert" → "Insert equation"

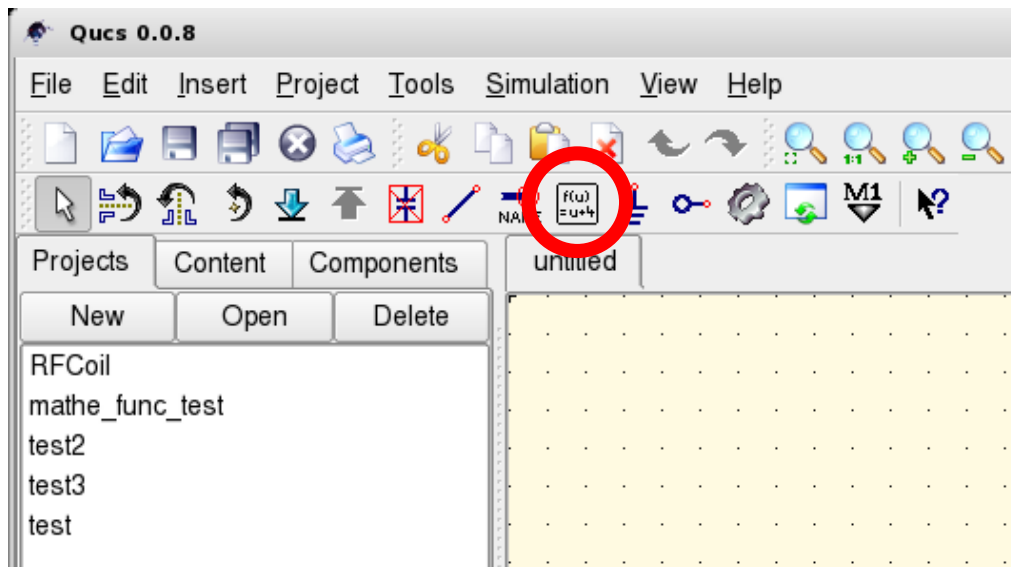


Figure 1: Entering a new measurement expression via equation icon

You can now place the equation symbol by mouse click anywhere in the schematic. Each mouse click creates a new equation instance each consisting of a variable number of measurement expressions. Press the **[Esc]** key if you do not like further equations.

Another option is to select an existing equation, copy it (either by menu item “Edit” → “Copy” or by **[Ctrl] + [C]**¹) and paste it (either by menu item “Edit” → “Paste” or by **[Ctrl] + [V]**).

After having successfully created an equation instance, you are now able to modify it.

Changing Measurement Expressions

For sake of simplicity we assume that you have just generated a new equation - if you like to change an existing, more complicated equation the following steps are the same.

Thus, the excerpt of your schematic surface looks like that in fig. 2.

¹ **[Ctrl] + [C]** means that you have to press the **[Ctrl]** key and the **[C]** key simultaneously.

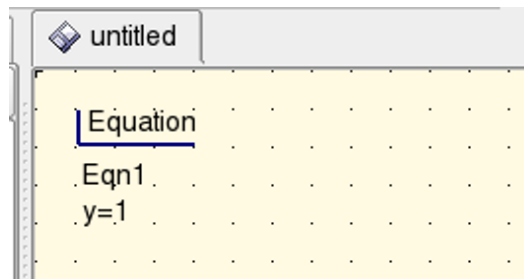


Figure 2: Newly created equation

You can now manipulate the current name of the equation instance. Simply click onto “Eqn1”, which becomes highlighted. Then type in a new name for it and finalise your inputs with the key.

After that, you can enter a new equation. Again, click onto “y=1”. Only the “1” is marked, and you can enter a new expression there. Please use the variables, operators and constants described in chapter “*Syntax of Measurement Expressions*”. Note that you can also refer to results (dependents) of other equations. But how to change the name of the current dependent “y”? Right click onto the equation, and a context menu opens. Select the first item called “Edit properties”. A sub window appears, which should look like the one in fig. 3. The alternative for entering equations is to double click onto the equation.

You can now change the name of the dependent, the equation itself (which is “1” in the example shown) and the name of the equation. If you do not want the result to be exported into the data display tab, but temporarily need it for further calculations, select “no” in the “Export value” cell.

Syntax of Measurement Expressions

Function names, variable names, and constant names are all case sensitive in measurement expressions - it is distinguished between lowercase and uppercase letters such as ‘a’ and ‘A’.

In functions, commas are used to separate arguments.

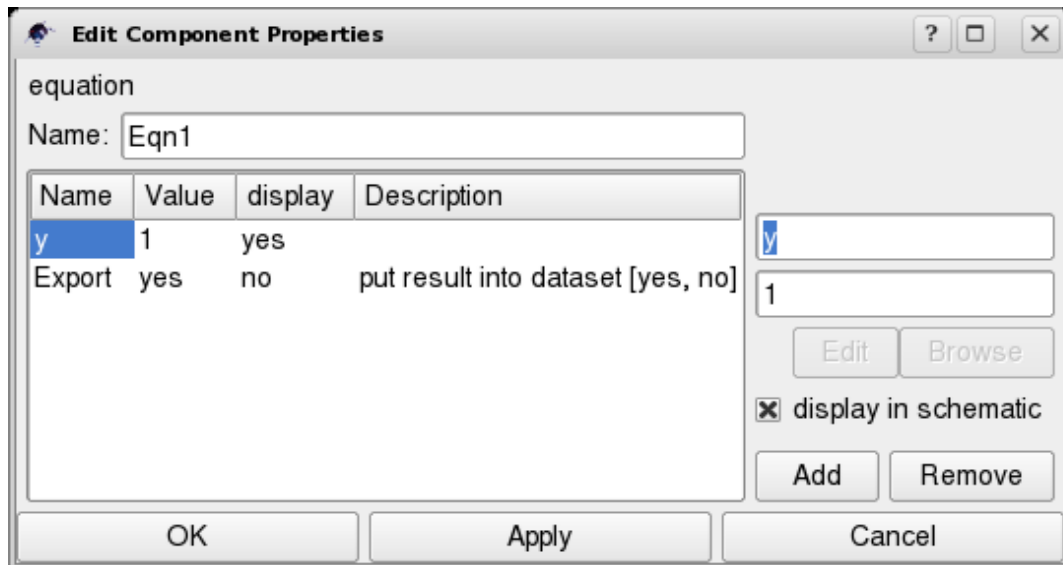


Figure 3: Editing equation properties

Variable Names

User defined variable names consist of a letter, followed by any number of letters, digits, or underscores.

The syntax of variable names created by the "Qucs" simulator is as specified in table 1. Please note that all voltages and currents in "Qucs" are peak values except the noise voltages and currents which are RMS values at 1Hz bandwidth.

Numbers

Numbers are written in conventional decimal way, with an optional decimal point between the digits. For powers of ten, the familiar scientific notation with an 'e' is used. In this way, '1.234e6' is an example for the real floating point number 1234000. Imaginary numbers can be entered by a multiplication factor 'i' or 'j' (see also table 3). An example would be '1+2*i' or - if you want to leave out the multiplication sign - '1+i2'.

Beside the scientific 'e' notation the following number suffixes can be used (see table 2):

| Variable Name | Description |
|--------------------|---|
| <i>nodename.V</i> | DC voltage at node <i>nodename</i> |
| <i>name.I</i> | DC current through circuit component <i>name</i> |
| <i>nodename.v</i> | AC voltage at node <i>nodename</i> |
| <i>name.i</i> | AC current through circuit component <i>name</i> |
| <i>nodename.vn</i> | AC noise voltage at node <i>nodename</i> |
| <i>name.in</i> | AC noise current through circuit component <i>name</i> |
| <i>nodename.Vt</i> | Transient voltage at node <i>nodename</i> |
| <i>name.It</i> | Transient current through circuit component <i>name</i> |
| <i>name.OP</i> | <i>name</i> = component name, OP = operating point (device dependent), e.g. D1.Id |
| S[x,y] | S-parameter, e.g. S[1,1] |
| Rn | equivalent noise resistance |
| Sopt | optimal reflection coefficient for minimum noise |
| Fmin | minimum noise figure |
| F | noise figure |
| <i>nodename.Vb</i> | Harmonic balance voltage at node <i>nodename</i> |

Table 1: Syntax of simulator generated variable names

Vectors and Matrices

You can enter vectors and matrices manually by enclosing columns and rows into brackets. Columns are separated by commas, rows by semicolons. A valid matrix entry in a measurement expression would be 'A=[1,2;3,4]', defining the matrix $A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$. The notation 'y=[1,2,3,4]' configures the vector $y = (1 \ 2 \ 3 \ 4)$. You get access to components of matrices and vectors by writing its name followed by brackets. Inside of the latter ranges (see table 6) or indices, separated by commas, define the extract you desire. Examples are 'y=M', accessing the whole matrix M , 'y=M[2,3]', extracting the value of the second row and third column of M , or 'y=M[:,3]', obtaining the complete third column.

Built-in Constants

The constants which can be used within measurement expressions are given in table 3.

| Suffix | Name | Value | Suffix | Name | Value |
|--------|------|-------|--------|-------|-------|
| E | exa | 1E+18 | m | milli | 1E-3 |
| P | peta | 1E+15 | u | micro | 1E-6 |
| T | tera | 1E+12 | n | nano | 1E-9 |
| G | giga | 1E+9 | p | pico | 1E-12 |
| M | mega | 1E+6 | f | femto | 1E-15 |
| k | kilo | 1E+3 | a | atto | 1E-18 |

Table 2: Number Suffixes

| Constant | Description | Value |
|----------|--------------------------------|-----------------|
| e | Euler's constant | 2.718282 |
| i , j | Imaginary unit ($\sqrt{-1}$) | il |
| kB | Boltzmann's constant | 1.380658e23 J/K |
| pi | π | 3.141593 |

Table 3: Built-in Constants

Operators

Operator Precedence Expressions are evaluated in the standard way, meaning from left to right, unless there are parentheses. The priority of operators is also handled familiarly, thus for example multiplication has precedence to addition. Tables 4 and 5 specify sorted lists of all operators, the topmost having highest priority. Operators on the same line have the same precedence.

Ranges The general nomenclature of ranges is displayed in table 6. It shows one-dimensional ranges, whereas also n-dimensional ranges are possible, if you consider nested sweeps.

Post Processing of Simulation Data by Expressions

After a simulation has run the results are stored in datasets. Usually, such a dataset is a vector or a matrix, but may also be a real or complex scalar. For transient analysis, this dataset contains voltage or current information over time, for Harmonic Balance it contains amplitudes at dedicated frequencies, while for S-parameter analysis a vector of matrices (thus matrices in dependency of frequency)

| Operator | Description | Example |
|----------|----------------------------|-----------|
| () | Parentheses, function call | y=max(v) |
| ^ | Exponentiation | y=3^4 |
| * | Multiplication | y=3*4 |
| / | Division | y=3/4 |
| % | Modulo | y=4%3 |
| + | Addition | y=3+4 |
| - | Subtraction | y=3-4 |
| : | Range operator | y=v[3:12] |
| +,- | Unary plus, unary minus | y=+x z=-y |

Table 4: Arithmetic Operator Priorities

is returned. In further generalisation the components of vectors and matrices consist of complex numbers.

Additionally, datasets can be generated by using expressions. As an example the linspace() function shall be named, which creates a vector of linearly spaced elements.

| Operator | Description | Example |
|----------|--|-----------------|
| () | Parentheses | $a=(x y)\&\&z$ |
| ! | Negation | $z=!x$ |
| ? : | Abbreviation for conditional expression "if x then y else z" | $a=x?y:z$ |
| && | And | $z=x\&\&y$ |
| | Or | $z=x y$ |
| ^^ | Exclusive Or | $z=x\wedge y$ |
| == | Equal | $z=x==y$ |
| != | Not equal | $z=x!=y$ |
| < | Less than | $z=x<y$ |
| <= | Less than or equal | $z=x<=y$ |
| > | Larger than | $z=x>y$ |
| >= | Larger than or equal | $z=x>=y$ |

Table 5: Logical Operator Priorities

| Syntax | Explanation |
|--------|-----------------------------------|
| m:n | Range from index m to index n |
| :n | Range up to index n |
| m: | Range starting from index m |
| : | No range limitations |

Table 6: Range definition

Functions Syntax and Overview

This chapter introduces the basic syntax of the function descriptions and contains a categorical list of all available functions.

Functions Reference Format

"Qucs" provides a rich set of functions, which can be used to generate and display new datasets by function based evaluation of simulation results. Beside a large number of mathematical standard functions such as square root (sqrt), exponential function (exp), absolute value (abs), functions especially useful for calculation and transformation of electronic values are implemented. Examples for the latter would be the conversion from Watts to dBm, the generation of noise circles in an amplifier

design, or the conversion from S-parameters to Y-parameters.

Functions Reference Format

In the subsequent two chapters, each function is described using the following structure:

<Function Name>

Outlines briefly the functionality of the function.

Syntax

Defines the general syntax of this function.

Arguments

Name, type, definition range and whether the argument is optional, are tabulated here. In case of an optional parameter the default value is specified. “Type” is a list defining the arguments allowed and may contain the following symbols:

| Symbol | Description |
|------------------------------------|---|
| \mathbb{R} | Real number |
| \mathbb{C} | Complex number |
| \mathbb{R}^n | Vector consisting of n real elements |
| \mathbb{C}^n | Vector consisting of n complex elements |
| $\mathbb{R}^{m \times n}$ | Real matrix consisting of m rows and n columns |
| $\mathbb{C}^{m \times n}$ | Complex matrix consisting of m rows and n columns |
| $\mathbb{R}^{m \times n \times p}$ | Vector of p real $m \times n$ matrices |
| $\mathbb{C}^{m \times n \times p}$ | Vector of p complex $m \times n$ matrices |

“Definition range” specifies the allowed range. Each range is introduced by a bracket, either “[” or “]”, meaning that the following start value of the range is either included or excluded. The start value is separated from the end value by a comma. Then the end value follows, finished by a bracket again, either “[” or “]”.

The first bracket mentioned means “excluding the end value”, the second means “including”.

If a range is given for a complex number, this specifies the real or imaginary value of that number. If a range is given for a real or complex vector or matrix, this specifies the real or imaginary value of each element of that vector or matrix. The symbols mean “includes listed value” and “excludes listed value”.

Description

Gives a more detailed description on what the function does and what it returns. In case some background knowledge is presented.

Examples

Shows an application of the function by one or several simple examples.

See also

Shows links to related functions. A mouse click onto the desired link leads to an immediate jump to that function.

Functions Listed by Category

This compilation shows all “Qucs” functions sorted by category (an alphabetical list is given in the appendix). Please click on the desired function to go to its detailed description.

Math Functions

Vectors and Matrices: Creation

| | | |
|-------------------------|-----|--|
| <code>eye()</code> | ... | Creates n x n identity matrix |
| <code>linspace()</code> | ... | Creates a real vector with linearly spaced components |
| <code>logspace()</code> | ... | Creates a real vector with logarithmically spaced components |

Vectors and Matrices: Basic Matrix Functions

| | | |
|--------------------------|-----|--------------------------|
| <code>adjoint()</code> | ... | Adjoint matrix |
| <code>array()</code> | ... | Read out single elements |
| <code>det()</code> | ... | Determinant of a matrix |
| <code>inverse()</code> | ... | Matrix inverse |
| <code>transpose()</code> | ... | Matrix transpose |
| <code>length()</code> | ... | Length of a vector |

Elementary Mathematical Functions: Basic Real and Complex Functions

| | | |
|------------------------|-----|---|
| <code>abs()</code> | ... | Absolute value |
| <code>angle()</code> | ... | Phase angle in radians of a complex number. Synonym for “arg” |
| <code>arg()</code> | ... | Phase angle in radians of a complex number |
| <code>conj()</code> | ... | Conjugate of a complex number |
| <code>deg2rad()</code> | ... | Converts phase from degrees into radians |
| <code>hypot()</code> | ... | Euclidean distance function |
| <code>imag()</code> | ... | Imaginary value of a complex number |
| <code>mag()</code> | ... | Magnitude of a complex number |
| <code>norm()</code> | ... | Square of the absolute value of a vector |
| <code>phase()</code> | ... | Phase angle in degrees of a complex number |
| <code>polar()</code> | ... | Transform from polar coordinates into complex number |
| <code>rad2deg()</code> | ... | Converts phase from degrees into radians |
| <code>real()</code> | ... | Real value of a complex number |
| <code>signum()</code> | ... | Signum function |
| <code>sign()</code> | ... | Sign function |
| <code>sqr()</code> | ... | Square of a number |
| <code>sqrt()</code> | ... | Square root |
| <code>unwrap()</code> | ... | Unwraps a phase vector in radians |

Elementary Mathematical Functions: Exponential and Logarithmic Functions

| | | |
|-----------------------|-----|-------------------------------|
| <code>exp()</code> | ... | Exponential function |
| <code>limexp()</code> | ... | Limited exponential function |
| <code>log10()</code> | ... | Decimal logarithm |
| <code>log2()</code> | ... | Binary logarithm |
| <code>ln()</code> | ... | Natural logarithm (base e) |

Elementary Mathematical Functions: Trigonometry

| | | |
|----------------------|-----|--------------------|
| <code>cos()</code> | ... | Cosine function |
| <code>cosec()</code> | ... | Cosecant |
| <code>cot()</code> | ... | Cotangent function |
| <code>sec()</code> | ... | Secant |
| <code>sin()</code> | ... | Sine function |
| <code>tan()</code> | ... | Tangent function |

Elementary Mathematical Functions: Inverse Trigonometric Functions

| | | |
|-------------------------|-----|---|
| <code>arccos()</code> | ... | Arc cosine (also known as “inverse cosine”) |
| <code>arccosec()</code> | ... | Arc cosecant (also known as “inverse cosecant”) |
| <code>arccot()</code> | ... | Arc cotangent |
| <code>arcsec()</code> | ... | Arc secant (also known as “inverse secant”) |
| <code>arcsin()</code> | ... | Arc sine (also known as “inverse sine”) |
| <code>arctan()</code> | ... | Arc tangent (also known as “inverse tangent”) |

Elementary Mathematical Functions: Hyperbolic Functions

| | | |
|-----------------------|-----|----------------------|
| <code>cosh()</code> | ... | Hyperbolic cosine |
| <code>cosech()</code> | ... | Hyperbolic cosecant |
| <code>coth()</code> | ... | Hyperbolic cotangent |
| <code>sech()</code> | ... | Hyperbolic secant |
| <code>sinh()</code> | ... | Hyperbolic sine |
| <code>tanh()</code> | ... | Hyperbolic tangent |

Elementary Mathematical Functions: Inverse Hyperbolic Functions

| | | |
|-------------------------|-----|---------------------------|
| <code>arcosh()</code> | ... | Hyperbolic area cosine |
| <code>arcosech()</code> | ... | Hyperbolic area cosecant |
| <code>arcoth()</code> | ... | Hyperbolic area cotangent |
| <code>arsech()</code> | ... | Hyperbolic area secant |
| <code>arsinh()</code> | ... | Hyperbolic area sine |
| <code>artanh()</code> | ... | Hyperbolic area tangent |

Elementary Mathematical Functions: Rounding

| | | |
|----------------------|-----|--|
| <code>ceil()</code> | ... | Round to the next higher integer |
| <code>fix()</code> | ... | Truncate decimal places from real number |
| <code>floor()</code> | ... | Round to the next lower integer |
| <code>round()</code> | ... | Round to nearest integer |

Elementary Mathematical Functions: Special Mathematical Functions

| | | |
|-------------------------|-----|---|
| <code>besseli0()</code> | ... | Modified Bessel function of order zero |
| <code>besselj()</code> | ... | Bessel function of n-th order |
| <code>bessely()</code> | ... | Bessel function of second kind and n-th order |
| <code>erf()</code> | ... | Error function |
| <code>erfc()</code> | ... | Complementary error function |
| <code>erfinv()</code> | ... | Inverse error function |
| <code>erfcinv()</code> | ... | Inverse complementary error function |
| <code>sinc()</code> | ... | Sinc function |
| <code>step()</code> | ... | Step function |

Data Analysis: Basic Statistics

| | | |
|------------|-----|--|
| avg() | ... | Average of vector elements |
| cumavg() | ... | Cumulative average of vector elements |
| max() | ... | Maximum value |
| min() | ... | Minimum value |
| rms() | ... | Root Mean Square of vector elements |
| runavg() | ... | Running average of vector elements |
| stddev() | ... | Standard deviation of vector elements |
| variance() | ... | Variance of vector elements |
| random() | ... | Random number between 0.0 and 1.0 |
| srandom() | ... | Set seed for a new series of pseudo-random numbers |

Data Analysis: Basic Operation

| | | |
|---------------|-----|---|
| cumprod() | ... | Cumulative product of vector elements |
| cumsum() | ... | Cumulative sum of vector elements |
| interpolate() | ... | Equidistant spline interpolation of data vector |
| prod() | ... | Product of vector elements |
| sum() | ... | Sum of vector elements |
| xvalue() | ... | Returns x-value which is associated with the y-value nearest to a specified y-value in a given vector |
| yvalue() | ... | Returns y-value of a given vector which is located nearest to the specified x-value |

Data Analysis: Differentiation and Integration

| | | |
|-------------|-----|--|
| ddx() | ... | Differentiate mathematical expression with respect to a given variable |
| diff() | ... | Differentiate vector with respect to another vector |
| integrate() | ... | Integrate vector |

Data Analysis: Signal Processing

| | | |
|-------------|-----|--|
| dft() | ... | Discrete Fourier Transform |
| fft() | ... | Fast Fourier Transform |
| idft() | ... | Inverse Discrete Fourier Transform |
| ifft() | ... | Inverse Fast Fourier Transform |
| fftshift() | ... | Move the frequency 0 to the center of the FFT vector |
| Time2Freq() | ... | Interpreted Discrete Fourier Transform |
| Freq2Time() | ... | Interpreted Inverse Discrete Fourier Transform |
| kbd() | ... | Kaiser-Bessel derived window |

Electronics Functions

Unit Conversion

| | | |
|---------|-----|--|
| dB() | ... | dB value |
| dbm() | ... | Convert voltage to power in dBm |
| dbm2w() | ... | Convert power in dBm to power in Watts |
| w2dbm() | ... | Convert power in Watts to power in dBm |

Reflection Coefficients and VSWR

| | | |
|----------|-----|---|
| rtoswr() | ... | Converts reflection coefficient to voltage standing wave ratio (VSWR) |
| rtoz() | ... | Converts reflection coefficient to admittance |
| rtoz() | ... | Converts reflection coefficient to impedance |
| ytor() | ... | Converts admittance to reflection coefficient |
| ztor() | ... | Converts impedance to reflection coefficient |

N-Port Matrix Conversions

| | | |
|-----------|-----|---|
| stos() | ... | Converts S-parameter matrix to S-parameter matrix with different reference impedance(s) |
| stoy() | ... | Converts S-parameter matrix to Y-parameter matrix |
| stoz() | ... | Converts S-parameter matrix to Z-parameter matrix |
| twoport() | ... | Converts a two-port matrix from one representation into another |
| ytos() | ... | Converts Y-parameter matrix to S-parameter matrix |
| ytoz() | ... | Converts Y-parameter matrix to Z-parameter matrix |
| ztos() | ... | Converts Z-parameter matrix to S-parameter matrix |
| ztoy() | ... | Converts Z-parameter matrix to Y-parameter matrix |

Amplifiers

| | | |
|---------------|-----|--|
| GaCircle() | ... | Circle(s) with constant available power gain Ga in the source plane |
| GpCircle() | ... | Circle(s) with constant operating power gain Gp in the load plane |
| Mu() | ... | Mu stability factor of a two-port S-parameter matrix |
| Mu2() | ... | Mu' stability factor of a two-port S-parameter matrix |
| NoiseCircle() | ... | Generates circle(s) with constant Noise Figure(s) |
| PlotVs() | ... | Returns a data item based upon vector or matrix vector with dependency on a given vector |
| Rollet() | ... | Rollet stability factor of a two-port S-parameter matrix |
| StabCircleL() | ... | Stability circle in the load plane |
| StabCircleS() | ... | Stability circle in the source plane |
| StabFactor() | ... | Stability factor of a two-port S-parameter matrix. Synonym for Rollet() |
| StabMeasure() | ... | Stability measure B1 of a two-port S-parameter matrix |
| vt() | ... | Thermal voltage for a given temperature in Kelvin |

Math Functions

Vectors and Matrices

Creation

eye()

Creates $n \times n$ identity matrix.

Syntax

`y=eye(n)`

Arguments

| Name | Type | Def. Range | Required |
|------|--------------|----------------|--------------|
| n | \mathbb{N} | $[1, +\infty[$ | \checkmark |

Description

This function creates the $n \times n$ identity matrix, that is

$$\begin{pmatrix} 1 & 0 & \cdots & 0 & 0 \\ 0 & 1 & 0 & \cdots & 0 \\ \vdots & 0 & \ddots & 0 & \vdots \\ 0 & \cdots & 0 & 1 & 0 \\ 0 & 0 & \cdots & 0 & 1 \end{pmatrix}$$

Example

`y=eye(2)` returns

| | |
|---|---|
| 1 | 0 |
| 0 | 1 |

.

See also

linspace()

Creates a real vector with linearly spaced components.

Syntax

`y=linspace(xs,xe,n)`

Arguments

| Name | Type | Def. Range | Required |
|------|--------------|-----------------------|----------|
| xs | \mathbb{R} | $] -\infty, +\infty[$ | ✓ |
| xe | \mathbb{R} | $] -\infty, +\infty[$ | ✓ |
| n | \mathbb{N} | $[2, +\infty[$ | ✓ |

Description

This function creates a real vector with n linearly spaced components. The first component is xs , the last one is xe .

Example

`y=linspace(1,2,3)` returns 1, 1.5, 2.

See also

`logspace()`

logspace()

Creates a real vector with logarithmically spaced components.

Syntax

`y=logspace(xs,xe,n)`

Arguments

| Name | Type | Def. Range | Required |
|------|--------------|-----------------------|--------------|
| xs | \mathbb{R} | $] -\infty, +\infty[$ | \checkmark |
| xe | \mathbb{R} | $] -\infty, +\infty[$ | \checkmark |
| n | \mathbb{N} | $[2, +\infty[$ | \checkmark |

Description

This function creates a real vector with n logarithmically spaced components. The first component is xs , the last one is xe .

Example

`y=logspace(1,2,3)` returns 1, 1.41, 2.

See also

`linspace()`

Basic Matrix Functions

adjoint()

Adjoint matrix.

Syntax

$Y = \text{adjoint}(X)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|----------------------|--------------|
| X | $\mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $]-\infty, +\infty[$ | \checkmark |

Description

This function calculates the adjoint matrix Y of a matrix X :

$Y = X^H = (X^*)^T$, where X^* is the complex conjugate matrix of X and X^T is the transposed of the matrix X .

Example

$X = \text{eye}(2) * (3+i)$ returns

| | |
|--------|--------|
| $3+j1$ | 0 |
| 0 | $3+j1$ |

. Then,

$Y = \text{adjoint}(X)$ returns

| | |
|--------|--------|
| $3-j1$ | 0 |
| 0 | $3-j1$ |

.

See also

[transpose\(\)](#), [conj\(\)](#)

array()

Read out single elements.

Syntax

The “array()” function is an implicit command. Thus normally the respective first expression (“preferred”) is used.

| Syntax | Preferred | Alternative | Preferred | Alternative |
|--------|-----------|-----------------|------------|------------------|
| 1 | y=VM[i,j] | y=array(VM,i,j) | | |
| 2 | y=M[i,j] | y=array(M,i,j) | | |
| 3 | y=VM[k] | y=array(VM,k) | | |
| 4 | y=v[i] | y=array(v,i) | y=v[r] | y=array(v,r) |
| 5 | y=v[i,r] | y=array(v,i,r) | y=v[r,j] | y=array(v,r,j) |
| | y=v[i,j] | y=array(v,i,j) | y=v[r1,r2] | y=array(v,r1,r2) |
| 6 | y=s[i] | y=array(s,i) | | |

Arguments

| Name | Type | Def. Range | Required |
|-----------|--|---|-------------------------|
| VM | $\mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $]-\infty, +\infty[$ | √(Syntax 1 and 3) |
| M | $\mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}$ | $]-\infty, +\infty[$ | √(Syntax 2) |
| v | $\mathbb{R}^n, \mathbb{C}^n$ | $]-\infty, +\infty[$ | √(Syntax 4 and 5) |
| r, r1, r2 | Range $xs : xe$ | $0 \leq xs \leq n-1, xs \leq xe \leq n-1$ | √(Syntax 4 and 5) |
| i | \mathbb{N} | $0 \leq i \leq m-1$ | √(Syntax 1, 2, 4, 5, 6) |
| j | \mathbb{N} | $0 \leq j \leq n-1$ | √(Syntax 1, 2, 5) |
| k | \mathbb{N} | $0 \leq k \leq p-1$ | √(Syntax 3) |
| s | String | Arbitrary characters | √(Syntax 6) |

Description

This function reads out real or complex vectors of matrices, matrices and vectors or strings. Please refer to the following table for the return values:

| Syntax | Argument 1 | Argument 2 | Argument 3 | Result |
|--|------------------|--------------------|--------------------|--|
| <code>y=VM[i,j]</code> | $VM = (x_{ijk})$ | $i \in \mathbb{N}$ | $j \in \mathbb{N}$ | Vector $(x_{ij1}, \dots, x_{ijK})$ |
| <code>y=M[i,j]</code> | $M = (x_{ij})$ | $i \in \mathbb{N}$ | $j \in \mathbb{N}$ | Number x_{ij} |
| <code>y=VM[k]</code> | $VM = (x_{ijk})$ | $k \in \mathbb{N}$ | | Matrix $\begin{pmatrix} x_{11k} & \cdots & x_{1nk} \\ \vdots & \ddots & \vdots \\ x_{m1k} & \cdots & x_{mnk} \end{pmatrix}$ |
| <code>y=v[i]</code> | $v = (v_i)$ | $i \in \mathbb{N}$ | | Number v_i |
| <code>y=v[xs:xe]</code> | $v = (v_i)$ | xs, \dots, xe | | Vector (v_{xs}, \dots, v_{xe}) |
| <code>y=v[i,xs:xe]</code> | $v = (v_i)$ | $i \in \mathbb{N}$ | xs, \dots, xe | Vector (v_{xs}, \dots, v_{xe}) |
| <code>y=v[xs:xe,j]</code> | $v = (v_i)$ | xs, \dots, xe | xs, \dots, xe | Vector (v_{xs}, \dots, v_{xe}) |
| <code>y=v[i,j]</code> | $v = (v_i)$ | $i \in \mathbb{N}$ | xs, \dots, xe | Vector (v_{xs}, \dots, v_{xe}) |
| <code>y=v[xs1:xe1, xs2:xe2]</code> | $v = (v_i)$ | $xs1, \dots, xe1$ | $xs2, \dots, xe2$ | Vector (v_{xs}, \dots, v_{xe}) |
| <code>y=s[i]</code> | $s = (s_i)$ | $i \in \mathbb{N}$ | | Character s_i |

Again, v denotes a vector, M a matrix, VM a vector of matrices, s a vector of characters and xs , $xs1$, $xs2$, xe , $xe1$, $xe2$ are range limiters.

Example

`v=linspace(1,2,4)` returns 1, 1.33, 1.67, 2. Then,

`y=v[3]` returns 2.

See also

det()

Determinant of a matrix.

Syntax

y=det(X)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| X | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | ✓ |

Description

This function calculates the determinant of a quadratical $n \times n$ matrix X. The result is either a real or a complex number.

Example

X=eye(2)*3 returns

| | |
|---|---|
| 3 | 0 |
| 0 | 3 |

. Then,

y=det(X) returns 9.

See also

eye()

inverse()

Matrix inverse.

Syntax

Y=inverse(X)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| X | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function inverts a quadratical $n \times n$ matrix X . The generated inverted matrix Y fulfills the equation

$X \cdot Y = X \cdot X^{-1} = 1$, where “ \cdot ” denotes matrix multiplication and “1” the identity matrix.

The matrix X must be regular, that means that its determinant $\Delta \neq 0$.

Example

X=eye(2)*3 returns

| | |
|---|---|
| 3 | 0 |
| 0 | 3 |

. Then,

Y=inverse(X) returns

| | |
|-------|-------|
| 0.333 | 0 |
| 0 | 0.333 |

.

See also

transpose(), eye(), det()

transpose()

Matrix transpose.

Syntax

$Y = \text{transpose}(X)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|----------------------|----------|
| X | $\mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $]-\infty, +\infty[$ | ✓ |

Description

This function transposes a $m \times n$ matrix X , which is equivalent to exchanging rows and columns according to

$$Y = X^T = (x_{ij})^T = (x_{ji}) \text{ with } 1 \leq i \leq m, 1 \leq j \leq n$$

The generated matrix Y is a $n \times m$ matrix.

Example

$X = \text{eye}(2) * 3$ returns

| | |
|---|---|
| 3 | 0 |
| 0 | 3 |

. Then,

$Y = \text{transpose}(X)$ returns

| | |
|---|---|
| 3 | 0 |
| 0 | 3 |

.

See also

[eye\(\)](#), [inverse\(\)](#)

length()

Length of a vector.

Syntax

`y=length(v)`

Arguments

| Name | Type | Def. Range | Required |
|----------------|--|----------------------|--------------|
| <code>v</code> | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $]-\infty, +\infty[$ | \checkmark |

Description

This function returns the length of vector v .

Example

`length(linspace(1,2,3))` returns 3.

See also

Elementary Mathematical Functions

Basic Real and Complex Functions

abs()

Absolute value.

Syntax

y=abs(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n, \mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $]-\infty, +\infty[$ | \checkmark |

Description

This function calculates the absolute value of a real or complex number, vector or matrix.

For $x \in \mathbb{R}$: $y = \begin{cases} x & \text{for } x \geq 0 \\ -x & \text{for } x < 0 \end{cases}$

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$: $y = \sqrt{a^2 + b^2}$

For x being a vector or a matrix the two equations above are applied to the components of x .

Examples

y=abs(-3) returns 3,

y=abs(-3+4*i) returns 5.

See also

`mag()`, `norm()`, `real()`, `imag()`, `conj()`, `phase()`, `arg()`, `hypot()`

angle()

Phase angle in radians of a complex number. Synonym for “arg”.

Syntax

```
y=angle(x)
```

See also

abs(), mag(), norm(), real(), imag(), conj(), phase(), arg()

arg()

Phase angle in radians of a complex number.

Syntax

$y = \arg(x)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n, \mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | ✓ |

Description

This function returns the phase angle in degrees of a real or complex number, vector or matrix.

For $x \in \mathbb{R}$: $y = \begin{cases} 0 & \text{for } x \geq 0 \\ \pi & \text{for } x < 0 \end{cases}$

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$:

| Definition range | Result |
|------------------|---|
| $a > 0, b > 0$ | $y = \arctan\left(\frac{b}{a}\right)$ |
| $a < 0, b > 0$ | $y = \arctan\left(\frac{b}{a}\right) + \pi$ |
| $a < 0, b < 0$ | $y = \arctan\left(\frac{b}{a}\right) - \pi$ |
| $a > 0, b < 0$ | $y = \arctan\left(\frac{b}{a}\right)$ |
| $a = 0, b > 0$ | $y = \frac{\pi}{2}$ |
| $a > 0, b = 0$ | $y = -\frac{\pi}{2}$ |
| $a = 0, b = 0$ | $y = 0$ |

In this case the $\arctan()$ function returns values in radians. The result y of the phase function is in the range $[-\pi, +\pi]$. For x being a vector or a matrix the two equations above are applied to the components of x .

Examples

`y=arg(-3)` returns 3.14,

`y=arg(-3+4*i)` returns 2.21.

See also

`abs()`, `mag()`, `norm()`, `real()`, `imag()`, `conj()`, `phase()`

conj()

Conjugate of a complex number.

Syntax

y=conj(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n, \mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | ✓ |

Description

This function returns the conjugate of a real or complex number, vector or matrix.

For $x \in \mathbb{R}$: $y = x$

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$: $y = a - i b$

For x being a vector or a matrix the two equations above are applied to the components of x .

Example

y=conj(-3+4*i) returns -3-4*i.

See also

abs(), mag(), norm(), real(), imag(), phase(), arg()

deg2rad()

Converts phase from degrees into radians.

Syntax

y=deg2rad(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function converts a real phase, a complex phase or a phase vector given in degrees into radians.

For $x \in \mathbb{R}$: $y = \frac{\pi}{180} x$

For $x \in \mathbb{C}$: $y = \frac{\pi}{180} \operatorname{Re}\{x\}$

For x being a vector the two equations above are applied to the components of x .

Example

y=deg2rad(45) returns 0.785.

See also

rad2deg(), phase(), arg()

hypot()

Euclidean distance function.

Syntax

`z=hypot(x,y)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |
| y | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function calculates the Euclidean distance z between two real or complex numbers or vectors. For two numbers $x, y \in \mathbb{C}$, this is

$$z = \sqrt{|x|^2 + |y|^2}$$

For x, y being vectors (of same size) the equation above is applied componentwise.

Examples

`z=hypot(3,4)` returns 5,

`z=hypot(1+2*i,1-2*i)` returns 3.16.

See also

`abs()`

imag()

Imaginary value of a complex number.

Syntax

y=imag(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n, \mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the imaginary value of a real or complex number, vector or matrix.

For $x \in \mathbb{R}$: $y = 0$

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$: $y = b$

For x being a vector or a matrix the two equations above are applied to the components of x .

Example

y=imag(-3+4*i) returns 4.

See also

abs(), mag(), norm(), real(), conj(), phase(), arg()

mag()

Magnitude of a complex number.

Syntax

y=mag(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n, \mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function calculates the magnitude (absolute value) of a real or complex number, vector or matrix.

$$\text{For } x \in \mathbb{R}: y = \begin{cases} x & \text{for } x \geq 0 \\ -x & \text{for } x < 0 \end{cases}$$

$$\text{For } \mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}: y = \sqrt{a^2 + b^2}$$

For x being a vector or a matrix the two equations above are applied to the components of x .

Examples

y=mag(-3) returns 3,

y=mag(-3+4*i) returns 5.

See also

abs(), norm(), real(), imag(), conj(), phase(), arg()

norm()

Square of the absolute value of a vector.

Syntax

y=norm(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the square of the absolute value of a real or complex number, vector or matrix.

For $x \in \mathbb{R}$: $y = x^2$

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$: $y = a^2 + b^2$

For x being a vector or a matrix the two equations above are applied to the components of x .

Example

y=norm(-3+4*i) returns 25.

See also

abs(), mag(), real(), imag(), conj(), phase(), arg()

phase()

Phase angle in degrees of a complex number.

Syntax

$y = \text{phase}(x)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n, \mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | ✓ |

Description

This function returns the phase angle in degrees of a real or complex number, vector or matrix.

For $x \in \mathbb{R}$: $y = \begin{cases} 0 & \text{for } x \geq 0 \\ 180 & \text{for } x < 0 \end{cases}$

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$:

| Definition range | Result |
|------------------|---|
| $a > 0, b > 0$ | $y = \arctan\left(\frac{b}{a}\right)$ |
| $a < 0, b > 0$ | $y = \arctan\left(\frac{b}{a}\right) + 180$ |
| $a < 0, b < 0$ | $y = \arctan\left(\frac{b}{a}\right) - 180$ |
| $a > 0, b < 0$ | $y = \arctan\left(\frac{b}{a}\right)$ |
| $a = 0, b > 0$ | $y = 90$ |
| $a > 0, b = 0$ | $y = -90$ |
| $a = 0, b = 0$ | $y = 0$ |

In this case the $\arctan()$ function returns values in degrees. The result y of the phase function is in the range $[-180, +180]$. For x being a vector or a matrix the two equations above are applied to the components of x .

Examples

`y=phase(-3)` returns 180,

`y=phase(-3+4*i)` returns 127.

See also

`abs()`, `mag()`, `norm()`, `real()`, `imag()`, `conj()`, `arg()`

polar()

Transform from polar coordinates into complex number.

Syntax

`c=polar(a,p)`

Arguments

| Name | Type | Def. Range | Required |
|------|------------------------------|-----------------------|----------|
| a | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |
| p | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function transforms a point given in polar coordinates (amplitude a and phase p in degrees) in the complex plane into the corresponding complex number:

$$x + i y = a e^{ip} = a \cos p + i a \sin p$$

For a or p being vectors the equation above is applied to the components of a or p .

Example

`c=polar(3,45)` returns 2.12+j2.12.

See also

`abs()`, `mag()`, `norm()`, `real()`, `imag()`, `conj()`, `phase()`, `arg()`, `exp()`, `cos()`, `sin()`

rad2deg()

Converts phase from degrees into radians.

Syntax

y=rad2deg(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function converts a real phase, a complex phase or a phase vector given in radians into degrees.

For $x \in \mathbb{R}$: $y = \frac{180}{\pi} x$

For $x \in \mathbb{C}$: $y = \frac{180}{\pi} \operatorname{Re}\{x\}$

For x being a vector the two equations above are applied to the components of x .

Example

y=rad2deg(45) returns 0.785.

See also

deg2rad(), phase(), arg()

real()

Real value of a complex number.

Syntax

`y=real(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n, \mathbb{R}^{m \times n}, \mathbb{C}^{m \times n}, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | ✓ |

Description

This function returns the real value of a real or complex number, vector or matrix.

For $x \in \mathbb{R}$: $y = x$

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$: $y = a$

For x being a vector or a matrix the two equations above are applied to the components of x .

Example

`y=real(-3+4*i)` returns -3.

See also

`abs()`, `mag()`, `norm()`, `imag()`, `conj()`, `phase()`, `arg()`

signum()

Signum function.

Syntax

y=signum(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function calculates the sign of a real or complex number or vector.

$$\text{For } x \in \mathbb{R}: y = \begin{cases} 1 & \text{for } x > 0 \\ 0 & \text{for } x = 0 \\ -1 & \text{for } x < 0 \end{cases}$$

$$\text{For } x \in \mathbb{C}: y = \begin{cases} \frac{x}{|x|} & \text{for } x \neq 0 \\ 0 & \text{for } x = 0 \end{cases}$$

For x being a vector the two equations above are applied to the components of x .

Examples

y=signum(-4) returns -1,

y=signum(3+4*i) returns 0.6+j0.8.

See also

abs(), sign()

sign()

Sign function.

Syntax

y=sign(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function calculates the sign of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \begin{cases} 1 & \text{for } x \geq 0 \\ -1 & \text{for } x < 0 \end{cases}$

For $x \in \mathbb{C}$: $y = \begin{cases} \frac{x}{|x|} & \text{for } x \neq 0 \\ 1 & \text{for } x = 0 \end{cases}$

For x being a vector the two equations above are applied to the components of x .

Examples

y=sign(-4) returns -1,

y=sign(3+4*i) returns 0.6+j0.8.

See also

abs(), signum()

sqr()

Square of a number.

Syntax

`y=sqr(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | $\sqrt{}$ |

Description

This function calculates the square root of a real or complex number or vector.

$$y = x^2$$

For x being a vector the two equations above are applied to the components of x .

Examples

`y=sqr(-4)` returns 16,

`y=sqr(3+4*i)` returns -7+j24.

See also

`sqrt()`

sqrt()

Square root.

Syntax

y=sqrt(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | $\sqrt{}$ |

Description

This function calculates the square root of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \begin{cases} \sqrt{x} & \text{for } x \geq 0 \\ i\sqrt{-x} & \text{for } x < 0 \end{cases}$

For $x \in \mathbb{C}$: $y = \sqrt{|x|} e^{i\frac{\varphi}{2}}$ with $\varphi = \arg(x)$

For x being a vector the two equations above are applied to the components of x .

Examples

y=sqrt(-4) returns 0+j2,

y=sqrt(3+4*i) returns 2+j1.

See also

sqr()

unwrap()

Unwraps a phase vector in radians.

Syntax

`y=unwrap(x)`

`y=unwrap(x, t)`

Arguments

| Name | Type | Def. Range | Required | Default |
|------|------------------------------|-----------------------|--------------|---------|
| x | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark | |
| t | \mathbb{R} | $] -\infty, +\infty[$ | | π |

Description

This function unwraps a phase vector x to avoid phase jumps. If two consecutive values of x differ by more than tolerance t , $\mp 2\pi$ (depending on the sign of the difference) is added to the current element of x . The predefined value of the optional parameter t is π .

Examples

`y=unwrap(3.15*linspace(-2,2,5))` returns -6.3, -9.43, -12.6, -15.7, -18.8,

`y=unwrap(2*linspace(-2,2,5),1)` returns -4, -8.28, -12.6, -16.8, -21.1,

`y=unwrap(2*linspace(-2,2,5),3)` returns -4, -2, 0, 2, 4.

See also

`abs()`, `mag()`, `norm()`, `real()`, `imag()`, `conj()`, `phase()`, `arg()`

Exponential and Logarithmic Functions

exp()

Exponential function.

Syntax

`y=exp(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function calculates the exponential function of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = e^x$

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$: $y = e^x = e^{a+ib} = e^a (\cos b + i \sin b)$

For x being a vector the two equations above are applied to the components of x .

Examples

`y=exp(-4)` returns 0.0183,

`y=exp(3+4*i)` returns -13.1-j15.2.

See also

`limexp()`, `ln()`, `log10()`, `log2()`, `cos()`, `sin()`

limexp()

Limited exponential function.

Syntax

`y=limexp(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function is equivalent to the exponential function $\exp(x)$, as long as $x \leq 80$. For larger arguments x , it limits the result to $y = \exp(80) \cdot (1 + x - 80)$. The argument can be a real or complex number or vector.

For $x \in \mathbb{R}$: $y = e^x$ for $x \leq 80$, $y = e^{80} \cdot (1 + x - 80)$ else.

For $\mathbb{C} \ni x := a + i b \wedge a, b \in \mathbb{R}$: $y = \limexp(x) = \limexp(a + i b) = \limexp(a) (\cos b + i \sin b)$

For x being a vector the two equations above are applied to the components of x .

Examples

`y=limexp(81)` returns 1.11e+35, whereas `y=exp(81)` returns 1.51e+35, which shows the limiting effect of the `limexp()` function.

`y=limexp(3+4*i)` returns -13.1-j15.2.

See also

`exp()`, `ln()`, `log10()`, `log2()`, `cos()`, `sin()`

log10()

Decimal logarithm.

Syntax

y=log10(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|---------------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[\setminus \{0\}$ | ✓ |

Description

This function calculates the principal value of the decimal logarithm (base 10) of a real or complex number or vector.

$$\text{For } x \in \mathbb{R}: y = \begin{cases} \frac{\ln(x)}{\ln(10)} & \text{for } x > 0 \\ \frac{\ln(-x)}{\ln(10)} + i \frac{\pi}{\ln(10)} & \text{for } x < 0 \end{cases}$$

$$\text{For } x \in \mathbb{C}: y = \frac{\ln(|x|)}{\ln(10)} + i \frac{\arg(x)}{\ln(10)}$$

For x being a vector the two equations above are applied to the components of x .

Examples

y=log10(-4) returns 0.602+j1.36,

y=log10(3+4*i) returns 0.699+j0.403.

See also

ln(), log2(), exp(), arg()

log2()

Binary logarithm.

Syntax

y=log2(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|---------------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[\setminus \{0\}$ | ✓ |

Description

This function calculates the principal value of the binary logarithm (base 2) of a real or complex number or vector.

$$\text{For } x \in \mathbb{R}: y = \begin{cases} \frac{\ln(x)}{\ln(2)} & \text{for } x > 0 \\ \frac{\ln(-x)}{\ln(2)} + i \frac{\pi}{\ln(2)} & \text{for } x < 0 \end{cases}$$

$$\text{For } x \in \mathbb{C}: y = \frac{\ln(|x|)}{\ln(2)} + i \frac{\arg(x)}{\ln(2)}$$

For x being a vector the two equations above are applied to the components of x .

Examples

y=log2(-4) returns 2+j4.53,

y=log2(3+4*i) returns 2.32+j1.34.

See also

ln(), log10(), exp(), arg()

ln()

Natural logarithm (base e).

Syntax

y=ln(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|---------------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[\setminus \{0\}$ | ✓ |

Description

This function calculates the principal value of the natural logarithm (base e) of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \begin{cases} \ln(x) & \text{for } x > 0 \\ \ln(-x) & \text{for } x < 0 \end{cases}$

For $x \in \mathbb{C}$: $y = \ln(|x|) + i \arg(x)$

For x being a vector the two equations above are applied to the components of x .

Examples

y=ln(-4) returns 1.39+j3.14,

y=ln(3+4*i) returns 1.61+j0.927.

See also

log2(), log10(), exp(), arg()

Trigonometry

cos()

Cosine function.

Syntax

`y=cos(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function calculates the cosine of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \cos(x)$ with $y \in [-1, 1]$

For $x \in \mathbb{C}$: $y = \frac{1}{2} (\exp(ix) + \exp(-ix))$

For x being a vector the two equations above are applied to the components of x .

Examples

`y=cos(-0.5)` returns 0.878,

`y=cos(3+4*i)` returns -27.0-j3.85.

See also

`sin()`, `tan()`, `arccos()`

cosec()

Cosecant.

Syntax

y=cosec(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|--|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[\setminus \{k\pi\}, k \in \mathbb{Z}$ | ✓ |

Description

This function calculates the cosecant of a real or complex number or vector.

$$y = \operatorname{cosec} x = \frac{1}{\sin x}$$

For x being a vector the equation above is applied to the components of x .

Example

y=cosec(1) returns 1.19.

See also

sin(), sec()

cot()

Cotangent function.

Syntax

`y=cot(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|--|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[\setminus \{k\pi\}, k \in \mathbb{Z}$ | ✓ |

Description

This function calculates the cotangent of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \frac{1}{\tan(x)}$ with $y \in [-\infty, +\infty]$

For $x \in \mathbb{C}$: $y = i \left(\frac{\exp(i x)^2 + 1}{\exp(i x)^2 - 1} \right)$

For x being a vector the two equations above are applied to the components of x .

Examples

`y=cot(-0.5)` returns -1.83,

`y=cot(3+4*i)` returns -0.000188-j1.

See also

`tan()`, `sin()`, `cos()`, `arctan()`, `arccot()`

sec()

Secant.

Syntax

y=sec(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|---|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[\setminus \left\{ \left(k + \frac{1}{2} \right) \pi \right\}, k \in \mathbb{Z}$ | ✓ |

Description

This function calculates the secant of a real or complex number or vector.

$$y = \sec x = \frac{1}{\cos x}$$

For x being a vector the equation above is applied to the components of x .

Example

y=sec(0) returns 1.

See also

cos(), cosec()

sin()

Sine function.

Syntax

y=sin(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function calculates the sine of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \sin(x)$ with $y \in [-1, 1]$

For $x \in \mathbb{C}$: $y = \frac{1}{2} i (\exp(-i x) - \exp(i x))$

For x being a vector the two equations above are applied to the components of x .

Examples

y=sin(-0.5) returns -0.479,

y=sin(3+4*i) returns 3.85-j27.

See also

cos(), tan(), arcsin()

tan()

Tangent function.

Syntax

y=tan(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|---|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[\setminus \left\{ \left(k + \frac{1}{2}\right) \pi \right\}, k \in \mathbb{Z}$ | ✓ |

Description

This function calculates the tangent of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \tan(x)$ with $y \in [-\infty, +\infty]$

For $x \in \mathbb{C}$: $y = -i \left(\frac{\exp(i x)^2 - 1}{\exp(i x)^2 + 1} \right)$

For x being a vector the two equations above are applied to the components of x .

Examples

y=tan(-0.5) returns -0.546,

y=tan(3+4*i) returns -0.000187+j0.999.

See also

cot(), sin(), cos(), arctan(), arccot()

Inverse Trigonometric Functions

arccos()

Arc cosine (also known as “inverse cosine”).

Syntax

$y = \arccos(x)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $[-1, +1]$ | \checkmark |

Description

This function calculates principal value of the the arc cosine of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \arccos(x)$ with $y \in [0, \pi]$

For $x \in \mathbb{C}$: $y = -i \ln(x + \sqrt{x^2 - 1})$

For x being a vector the two equations above are applied to the components of x .

Examples

$y = \arccos(-1)$ returns 3.14,

$y = \arccos(3+4*i)$ returns 0.937-j2.31.

See also

$\cos()$, $\arcsin()$, $\arctan()$, $\text{arccot}()$

arccosec()

Arc cosecant (also known as “inverse cosecant”).

Syntax

`y=arccosec(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $\mathbb{C} \setminus \{0\}$ | ✓ |

Description

This function calculates the principal value of the the arc cosecant of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \arccosec(x)$ with $y \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$

For $x \in \mathbb{C}$: $y = -i \ln \left[\sqrt{1 - \frac{1}{x^2}} + \frac{i}{x} \right]$

For x being a vector the two equations above are applied to the components of x .

Examples

`y=arccosec(-1)` returns -1.57,

`y=arccosec(3+4*i)` returns 0.119-j0.16.

See also

`cosec()`, `arcsec()`

arccot()

Arc cotangent.

Syntax

y=arccot(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function calculates the principal value of the arc cotangent of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \text{arccot}(x)$ with $y \in [0, \pi]$

For $x \in \mathbb{C}$: $y = \frac{i}{2} \ln \left(\frac{x-i}{x+i} \right)$

For x being a vector the two equations above are applied to the components of x .

Examples

y=arccot(-1) returns 2.36,

y=arccot(3+4*i) returns 0.122-j0.159.

See also

cot(), tan(), arccos(), arcsin(), arctan()

arcsec()

Arc secant (also known as “inverse secant”).

Syntax

y=arcsec(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|------------------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $\mathbb{C} \setminus \{0\}$ | \checkmark |

Description

This function calculates the principal value of the arc secant of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \text{arcsec}(x)$ with $y \in [0, \pi]$

For $x \in \mathbb{C}$: $y = \frac{\pi}{2} + i \ln \left[\sqrt{1 - \frac{1}{x^2}} + \frac{i}{x} \right]$

For x being a vector the two equations above are applied to the components of x .

Examples

y=arcsec(-1) returns 3.14,

y=arcsec(3+4*i) returns 1.45+j0.16.

See also

sec(), arccosec()

arcsin()

Arc sine (also known as “inverse sine”).

Syntax

y=arcsin(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $[-1, +1]$ | ✓ |

Description

This function calculates the principal value of the arc sine of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \arcsin(x)$ with $y \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$

For $x \in \mathbb{C}$: $y = -i \ln \left[i x + \sqrt{1 - x^2} \right]$

For x being a vector the two equations above are applied to the components of x .

Examples

y=arcsin(-1) returns -1.57,

y=arcsin(3+4*i) returns 0.634+j2.31.

See also

sin(), arccos(), arctan(), arccot()

arctan()

Arc tangent (also known as “inverse tangent”).

Syntax

$z = \arctan(x)$

$z = \arctan(y, x)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |
| y | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | |

Description

For the first syntax ($z = \arctan(x)$), this function calculates the principal value of the arc tangent of a real or complex number or vector.

For $x \in \mathbb{R}$: $y = \arctan(x)$ with $y \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$

For $x \in \mathbb{C}$: $y = -\frac{1}{2}i \ln \left[\frac{2i}{x+i} - 1 \right]$

For x being a vector the two equations above are applied to the components of x .

If the second syntax ($z = \arctan(y, x)$) finds application, the expression

$$z = \pm \arctan(y/x)$$

(with the $\arctan()$ function defined above) is evaluated. The sign of z is determined by

$$\text{sign}(z) = \begin{cases} + & \text{for } \text{Re}\{x\} > 0 \\ - & \text{for } \text{Re}\{x\} < 0 \end{cases} .$$

Note that for the second syntax the case $x = y = 0$ is not defined.

Examples

`z=arctan(-1)` returns -0.785,

`z=arctan(3+4*i)` returns 1.45+j0.159,

`z=arctan(1,1)` returns 0.785.

See also

`tan()`, `arccos()`, `arcsin()`, `arccot()`

Hyperbolic Functions

cosh()

Hyperbolic cosine.

Syntax

y=cosh(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function calculates the hyperbolic cosine of a real or complex number or vector.

$$y = \frac{1}{2} (e^x + e^{-x})$$

For x being a vector the equation above is applied to the components of x .

Examples

y=cosh(-1) returns 1.54,

y=cosh(3+4*i) returns -6.58-j7.58.

See also

exp(), sinh(), tanh(), cos()

cosech()

Hyperbolic cosecant.

Syntax

`y=cosech(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-------------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $]-\infty, +\infty[\setminus \{0\}$ | ✓ |

Description

This function calculates the hyperbolic cosecant of a real or complex number or vector.

$$y = \frac{1}{\sinh x}$$

For x being a vector the equation above is applied to the components of x .

Examples

`y=cosech(-1)` returns -0.851,

`y=cosech(3+4*i)` returns -0.0649+j0.0755.

See also

`exp()`, `sinh()`, `sech()`, `cosec()`

coth()

Hyperbolic cotangent.

Syntax

y=coth(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|---------------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[\setminus \{0\}$ | ✓ |

Description

This function calculates the hyperbolic cotangent of a real or complex number or vector.

$$y = \frac{1}{\tanh x} = \frac{e^x + e^{-x}}{e^x - e^{-x}}$$

For x being a vector the equation above is applied to the components of x .

Examples

y=coth(-1) returns -1.31,

y=coth(3+4*i) returns 0.999-j0.0049.

See also

exp(), cosh(), sinh(), tanh(), tan()

sech()

Hyperbolic secant.

Syntax

y=sech(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function calculates the hyperbolic secant of a real or complex number or vector.

$$y = \frac{1}{\cosh x}$$

For x being a vector the equation above is applied to the components of x .

Examples

y=sech(-1) returns 0.648,

y=sech(3+4*i) returns -0.0653+j0.0752.

See also

exp(), cosh(), cosech(), sec()

sinh()

Hyperbolic sine.

Syntax

y=sinh(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function calculates the hyperbolic sine of a real or complex number or vector.

$$y = \frac{1}{2} (e^x - e^{-x})$$

For x being a vector the equation above is applied to the components of x .

Examples

y=sinh(-1) returns -1.18,

y=sinh(3+4*i) returns -6.55-j7.62.

See also

exp(), cosh(), tanh(), sin()

tanh()

Hyperbolic tangent.

Syntax

y=tanh(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function calculates the hyperbolic tangent of a real or complex number or vector.

$$y = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

For x being a vector the equation above is applied to the components of x .

Examples

y=tanh(-1) returns -0.762,

y=tanh(3+4*i) returns 1+j0.00491.

See also

exp(), cosh(), sinh(), coth(), tan()

Inverse Hyperbolic Functions

arcosh()

Hyperbolic area cosine.

Syntax

y=arcosh(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|----------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $[1, +\infty[$ | \checkmark |

Description

This function calculates the hyperbolic area cosine of a real or complex number or vector, which is the inverse function to the “cosh” function.

$$y = \operatorname{arcosh} x = \ln \left(x + \sqrt{x^2 - 1} \right)$$

For x being a vector the equation above is applied to the components of x .

Examples

y=arcosh(1) returns 0,

y=arcosh(3+4*i) returns 2.31+j0.937.

See also

arsinh(), artanh(), cosh(), arccos(), ln(), sqrt()

arcosech()

Hyperbolic area cosecant.

Syntax

y=arcosech(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $\mathbb{C} \setminus \{0\}$ | ✓ |

Description

This function calculates the hyperbolic area cosecant of a real or complex number or vector, which is the inverse function to the “cosech” function.

For $x \in \mathbb{C} \setminus \{0\}$: $y = \ln \left(\sqrt{1 + \frac{1}{x^2}} + \frac{1}{x} \right)$

For x being a vector the equation above is applied to the components of x .

Examples

y=arcosech(1) returns 0.881,

y=arcosech(i) returns -i1.57.

See also

cosech(), arsech(), ln(), sqrt()

arcoth()

Hyperbolic area cotangent.

Syntax

y=arcoth(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-------------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, -1[\cup] 1, +\infty[$ | ✓ |

Description

This function calculates the hyperbolic area cotangent of a real or complex number or vector, which is the inverse function to the “cotanh” function.

$$y = \operatorname{arcoth} x = \frac{1}{2} \ln \left(\frac{x+1}{x-1} \right)$$

For x being a vector the equation above is applied to the components of x .

Examples

y=arcoth(2) returns 0.549,

y=arcoth(3+4*i) returns 0.118-j0.161.

See also

arsinh(), arcosh(), tanh(), arctan(), ln(), sqrt()

arsech()

Hyperbolic area secant.

Syntax

y=arsech(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|------------------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $\mathbb{C} \setminus \{0\}$ | ✓ |

Description

This function calculates the hyperbolic area secant of a real or complex number or vector, which is the inverse function to the “sech” function.

For $x \in \mathbb{C} \setminus \{0\}$: $y = \ln \left(\sqrt{\frac{1}{x} - 1} \sqrt{\frac{1}{x} + 1} + \frac{1}{x} \right)$

For x being a vector the equation above is applied to the components of x .

Examples

y=arsech(1) returns 0,

y=arsech(3+4*i) returns 0.16-j1.45.

See also

sech(), arcosech(), ln(), sqrt()

arsinh()

Hyperbolic area sine.

Syntax

y=arsinh(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function calculates the hyperbolic area sine of a real or complex number or vector, which is the inverse function to the “sinh” function.

$$y = \operatorname{arsinh} x = \ln \left(x + \sqrt{x^2 + 1} \right)$$

For x being a vector the equation above is applied to the components of x .

Examples

y=arsinh(1) returns 0.881,

y=arsinh(3+4*i) returns 2.3+j0.918.

See also

arcosh(), artanh(), sinh(), arcsin(), ln(), sqrt()

artanh()

Hyperbolic area tangent.

Syntax

y=artanh(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -1, +1[$ | ✓ |

Description

This function calculates the hyperbolic area tangent of a real or complex number or vector, which is the inverse function to the “tanh” function.

$$y = \operatorname{artanh} x = \frac{1}{2} \ln \left(\frac{1+x}{1-x} \right)$$

For x being a vector the equation above is applied to the components of x .

Examples

y=artanh(0) returns 0,

y=artanh(3+4*i) returns 0.118+j1.41.

See also

arsinh(), arcosh(), tanh(), arctan(), ln(), sqrt()

Rounding

ceil()

Round to the next higher integer.

Syntax

`y=ceil(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function rounds a real number x to the next higher integer value.

If x is a complex number both real part and imaginary part are rounded. For x being a vector the operation above is applied to the components of x .

Examples

`y=ceil(-3.5)` returns -3,

`y=ceil(3.2+4.7*i)` returns 4+j5.

See also

`floor()`, `fix()`, `round()`

fix()

Truncate decimal places from real number.

Syntax

$y = \text{fix}(x)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function truncates the decimal places from a real number x and returns an integer.

If x is a complex number both real part and imaginary part are rounded. For x being a vector the operation above is applied to the components of x .

Examples

$y = \text{fix}(-3.5)$ returns -3,

$y = \text{fix}(3.2 + 4.7 \cdot i)$ returns $3 + j4$.

See also

`ceil()`, `floor()`, `round()`

floor()

Round to the next lower integer.

Syntax

`y=floor(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function rounds a real number x to the next lower integer value.

If x is a complex number both real part and imaginary part are rounded. For x being a vector the operation above is applied to the components of x .

Examples

`y=floor(-3.5)` returns -4,

`y=floor(3.2+4.7*i)` returns 3+j4.

See also

`ceil()`, `fix()`, `round()`

round()

Round to nearest integer.

Syntax

`y=round(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function rounds a real number x to its nearest integer value.

If x is a complex number both real part and imaginary part are rounded. For x being a vector the operation above is applied to the components of x .

Examples

`y=round(-3.5)` returns -4,

`y=round(3.2+4.7*i)` returns 3+j5.

See also

`ceil()`, `floor()`, `fix()`

Special Mathematical Functions

besseli0()

Modified Bessel function of order zero.

Syntax

i0=besseli0(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $]-\infty, +\infty[$ | \checkmark |

Description

This function evaluates the modified Bessel function of order zero of a real or complex number or vector.

$$i0(x) = J_0(ix) = \sum_{k=0}^{\infty} \frac{\left(\frac{x}{2}\right)^{2k}}{k! \Gamma(k+1)},$$

where $J_0(x)$ is the Bessel function of order zero and $\Gamma(x)$ denotes the gamma function.

For x being a vector the equation above is applied to the components of x .

Example

y=besseli0(1) returns 1.266.

See also

besselj(), bessely()

besselj()

Bessel function of n-th order.

Syntax

jn=besselj(n,x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| n | \mathbb{N} | $[0, +\infty[$ | \checkmark |
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function evaluates the Bessel function of n-th order of a real or complex number or vector.

$$J_n(x) = \sum_{k=0}^{\infty} \frac{(-1)^k \left(\frac{x}{2}\right)^{n+2k}}{k! \Gamma(n+k+1)},$$

where $\Gamma(x)$ denotes the gamma function.

For x being a vector the equation above is applied to the components of x .

Example

y=besselj(1,1) returns 0,44.

See also

besseli0(), bessely()

bessely()

Bessel function of second kind and n-th order.

Syntax

yn=bessely(n,x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| n | N | $[0, +\infty[$ | ✓ |
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function evaluates the Bessel function of second kind and n-th order of a real or complex number or vector.

$$Y_n(x) = \lim_{m \rightarrow n} \frac{J_m(x) \cos m\pi - J_{-m}(x)}{\sin m\pi},$$

where $J_m(x)$ denotes the Bessel function of first kind and n-th order.

For x being a vector the equation above is applied to the components of x .

Example

y=bessely(1,1) returns -0.781.

See also

besseli0(), besselj()

erf()

Error function.

Syntax

y=erf(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function evaluates the error function of a real or complex number or vector.
For $x \in \mathbb{R}$,

$$y = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$$

If x is a complex number both real part and imaginary part are subjected to the equation above. For x being a vector the equation is applied to the components of x .

Example

y=erf(0.5) returns 0.520.

See also

erfc(), erfinv(), erfcinv(), exp()

erfc()

Complementary error function.

Syntax

`y=erfc(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function evaluates the complementary error function of a real or complex number or vector. For $x \in \mathbb{R}$,

$$y = 1 - \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$$

If x is a complex number both real part and imaginary part are subjected to the equation above. For x being a vector the equation is applied to the components of x .

Example

`y=erfc(0.5)` returns 0.480.

See also

`erf()`, `erfinv()`, `erfcinv()`, `exp()`

erfinv()

Inverse error function.

Syntax

`y=erfinv(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -1, +1[$ | \checkmark |

Description

This function evaluates the inverse of the error function of a real or complex number or vector. For $-1 < x < 1$,

$$y = \operatorname{erf}^{-1}(x)$$

If x is a complex number both real part and imaginary part are subjected to the equation above. For x being a vector the equation is applied to the components of x .

Example

`y=erfinv(0.8)` returns 0.906.

See also

`erf()`, `erfc()`, `erfcinv()`, `exp()`

erfcinv()

Inverse complementary error function.

Syntax

`y=erfcinv(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $]0, +2[$ | \checkmark |

Description

This function evaluates the inverse of the complementary error function of a real or complex number or vector. For $0 < x < 2$,

$$y = \operatorname{erfc}^{-1}(x)$$

If x is a complex number both real part and imaginary part are subjected to the equation above. For x being a vector the equation is applied to the components of x .

Example

`y=erfcinv(0.5)` returns 0.477.

See also

`erf()`, `erfc()`, `erfinv()`, `exp()`

sinc()

Sinc function.

Syntax

y=sinc(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function evaluates the sinc function of a real or complex number or vector.

$$y = \begin{cases} \frac{\sin x}{x} & \text{for } x \neq 0 \\ 1 & \text{for } x = 0 \end{cases}$$

For x being a vector the equation above is applied to the components of x .

Examples

y=sinc(-3) returns 0.047,

y=sinc(3+4*i) returns -3.86-j3.86.

See also

sin()

step()

Step function.

Syntax

y=step(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function calculates the step function of a real or complex number or vector.
For $x \in \mathbb{R}$,

$$y = \begin{cases} 0 & \text{for } x < 0 \\ 0.5 & \text{for } x = 0 \\ 1 & \text{for } x > 0 \end{cases}$$

If x is a complex number both real part and imaginary part are subjected to the equation above. For x being a vector the equation is applied to the components of x .

Example

y=step(0.5) returns 1.

See also

Data Analysis

Basic Statistics

avg()

Average of vector elements.

Syntax

y=avg(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$, Range $xs : xe$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the sum of the elements of a real or complex vector or range.

For $x \in \mathbb{C}^n$: $y = \frac{1}{n} \sum_{i=1}^n x_i$, $1 \leq i \leq n$ (for vectors) or $xs \leq i \leq xe$ (for ranges)

For x being a real or complex number, x itself is returned.

Example

y=avg(linspace(1,3,10)) returns 2.

See also

sum(), max(), min()

cumavg()

Cumulative average of vector elements.

Syntax

y=cumavg(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the cumulative average of the elements of a real or complex vector.

For $x \in \mathbb{C}^n$: $y_k = \frac{1}{k} \sum_{i=1}^k x_i, 1 \leq k \leq n$

For x being a real or complex number, x itself is returned.

Example

y=cumavg(linspace(1,3,3)) returns 1, 1.5, 2.

See also

cumsum(), cumprod(), avg(), sum(), prod(), max(), min()

max()

Maximum value.

Syntax

y=max(x)

y=max(a,b)

Arguments

| Name | Type | Def. Range | Required |
|------|---|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n, \text{Range } xs : xe$ | $] -\infty, +\infty[$ | ✓ |
| a | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | ✓ |
| b | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | ✓ |

Description

For the first syntax (y=max(x)), this function returns the maximum value of a real or complex vector or range.

For $x \in \mathbb{R}^n$: $y = \max(x_i)$, $1 \leq i \leq n$ (for vectors) or $xs \leq i \leq xe$ (for ranges)

For $x \in \mathbb{C}^n$: $y = \max(\pm |x_i|)$, $1 \leq i \leq n$ (for vectors) or $xs \leq i \leq xe$ (for ranges),

with sign $\begin{cases} + & \text{for } |\arg(x_i)| \leq \frac{\pi}{2} \\ - & \text{else} \end{cases}$

For x being a real or complex number: that is the case $n = 1$.

The second syntax (y=max(a,b)) finds application, if two (generally complex) numbers a and b need to be compared. In principle, the maximum of the absolute values is selected, but it must be considered whether a and b are located in the right or left complex half plane. If the latter is the case, the negative absolute

value of a and b needs to be regarded (for example, which is the case for negative real numbers), otherwise the positive absolute value is taken:

$$y = \max(\pm |a|, \pm |b|),$$

$$\text{with } |a| \text{ sign } \begin{cases} + & \text{for } |\arg(a)| \leq \frac{\pi}{2} \\ - & \text{else} \end{cases} \text{ and } |b| \text{ sign } \begin{cases} + & \text{for } |\arg(b)| \leq \frac{\pi}{2} \\ - & \text{else} \end{cases}$$

Example

`y=max(linspace(1,3,10))` returns 3.

`y=max(1,3)` returns 3.

`y=max(1,1+i)` returns $1+j1$.

`y=max(1,-1+i)` returns 1.

See also

`min()`, `abs()`

min()

Minimum value.

Syntax

y=min(x)

y=min(a,b)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$, Range $xs : xe$ | $] -\infty, +\infty[$ | ✓ |
| a | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | ✓ |
| b | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | ✓ |

Description

For the first syntax (y=min(x)), this function returns the minimum value of a real or complex vector or range.

For $x \in \mathbb{R}^n$: $y = \min(x_i)$, $1 \leq i \leq n$ (for vectors) or $xs \leq i \leq xe$ (for ranges)

For $x \in \mathbb{C}^n$: $y = \min(\pm |x_i|)$, $1 \leq i \leq n$ (for vectors) or $xs \leq i \leq xe$ (for ranges),

with sign $\begin{cases} + & \text{for } |\arg(x_i)| \leq \frac{\pi}{2} \\ - & \text{else} \end{cases}$

For x being a real or complex number: that is the case $n = 1$.

The second syntax (y=min(a,b)) finds application, if two (generally complex) numbers a and b need to be compared. In principle, the maximum of the absolute values is selected, but it must be considered whether a and b are located in the right or left complex half plane. If the latter is the case, the negative absolute

value of a and b needs to be regarded (for example, which is the case for negative real numbers), otherwise the positive absolute value is taken:

$$y = \min(\pm |a|, \pm |b|),$$

$$\text{with } |a| \text{ sign } \begin{cases} + & \text{for } |\arg(a)| \leq \frac{\pi}{2} \\ - & \text{else} \end{cases} \text{ and } |b| \text{ sign } \begin{cases} + & \text{for } |\arg(b)| \leq \frac{\pi}{2} \\ - & \text{else} \end{cases}$$

Example

`y=min(linspace(1,3,10))` returns 1.

`y=min(1,3)` returns 1.

`y=min(1,1+i)` returns 1.

`y=min(1,-1+i)` returns -1+j1.

See also

`max()`, `abs()`

rms()

Root Mean Square of vector elements.

Syntax

y=rms(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the rms (root mean square) value of the elements of a real or complex vector. By application of the trapezoidal integration rule,

$$\text{for } x \in \mathbb{C}^n: y = \sqrt{\frac{1}{n} \sum_{i=1}^n a_i x_i x_i^*}, \quad 1 \leq i \leq n, \quad a_i = \begin{cases} 1 & \text{for } 2 \leq i \leq n-1 \\ \frac{1}{2} & \text{for } i = 1 \text{ or } i = n \end{cases}$$

For x being a real or complex number, $|x|$ itself is returned.

Example

y=rms(linspace(1,2,8)) returns 1.43.

See also

variance(), stddev(), avg()

runavg()

Running average of vector elements.

Syntax

`y=runavg(x,m)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |
| m | \mathbb{N} | $[1, +\infty[$ | ✓ |

Description

This function returns the running average over m elements of a real or complex vector.

For $x \in \mathbb{C}^n$: $y_k = \frac{1}{m} \sum_{i=k}^{k+m-1} x_i, 1 \leq k \leq n$

For x being a real or complex number, x itself is returned.

Example

`y=runavg(linspace(1,3,6),2)` returns 1.2, 1.6, 2, 2.4, 2.8.

See also

`cumavg()`, `cumsum()`, `avg()`, `sum()`

stddev()

Standard deviation of vector elements.

Syntax

`y=stddev(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the stddev of the elements of a real or complex vector x .

For $x \in \mathbb{C}^n$: $y = \sqrt{\text{variance}(x)}$

For x being a real or complex number, 0 is returned.

Example

`y=stddev(linspace(1,3,10))` returns 0.673.

See also

`stddev()`, `avg()`, `max()`, `min()`

variance()

Variance of vector elements.

Syntax

y=variance(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the variance of the elements of a real or complex vector.

For $x \in \mathbb{C}^n$: $y = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$, where \bar{x} denotes mean (average) value of x .

For x being a real or complex number, 0 is returned.

Example

y=variance(linspace(1,3,10)) returns 0.453.

See also

stddev(), avg(), max(), min()

random()

Random number between 0.0 and 1.0.

Syntax

```
y=random()
```

Arguments

None.

Description

This function returns a pseudo-random real number between 0.0 (including) and 1.0 (excluding). The starting point of the random number generator can be set by `srandom()`.

Example

```
y=random()
```

See also

`srandom()`

srandom()

Set seed for a new series of pseudo-random numbers.

Syntax

y=srandom(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--------------|-----------------------|----------|
| x | \mathbb{R} | $] -\infty, +\infty[$ | ✓ |

Description

This function establishes x as the seed for a new series of pseudo-random numbers. Please note that only integer values for x are considered, so for example $x = 1.1$ will give the same seed as $x = 1$.

Example

y=srandom(100)

See also

random()

Basic Operation

cumprod()

Cumulative product of vector elements.

Syntax

`y=cumprod(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the cumulative product of the elements of a real or complex vector.

For $x \in \mathbb{C}^n$: $y_k = \prod_{i=1}^k x_i, 1 \leq k \leq n$

For x being a real or complex number, x itself is returned.

Example

`y=cumprod(linspace(1,3,3))` returns 1, 2, 6.

See also

`cumsum()`, `cumavg()`, `prod()`, `sum()`, `avg()`, `max()`, `min()`

cumsum()

Cumulative sum of vector elements.

Syntax

`y=cumsum(x)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function returns the cumulative sum of the elements of a real or complex vector.

For $x \in \mathbb{C}^n$: $y_k = \sum_{i=1}^k x_i, 1 \leq k \leq n$

For x being a real or complex number, x itself is returned.

Example

`y=cumsum(linspace(1,3,3))` returns 1, 3, 6.

See also

`cumprod()`, `cumavg()`, `sum()`, `prod()`, `avg()`, `max()`, `min()`

interpolate()

Equidistant spline interpolation of data vector.

Syntax

`z=interpolate(y,t,m)`

`z=interpolate(y,t)`

Arguments

| Name | Type | Def. Range | Required | Default |
|------|------------------------------|-----------------------|----------|---------|
| y | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ | |
| t | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ | |
| m | \mathbb{N} | $[3, +\infty[$ | | 64 |

Description

This function uses spline interpolation to interpolate between the points of a vector $y(t)$. If the number of samples n is not specified, a default value of $n = 64$ is assumed.

Example

`z=interpolate(linspace(0,2,3)*linspace(0,2,3),linspace(0,2,3))`

returns a smooth parabolic curve:

Use the Cartesian diagram to display it.

See also

`sum()`, `prod()`

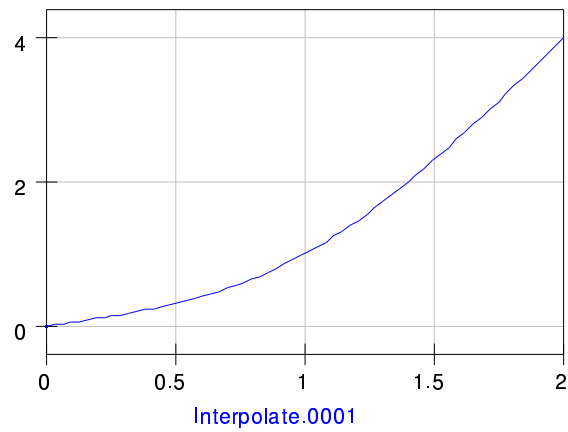


Figure 4: Interpolated curve

prod()

Product of vector elements.

Syntax

$y = \text{prod}(x)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the product of the elements of a real or complex vector.

For $x \in \mathbb{C}^n$: $y = \prod_{i=1}^n x_i$

For x being a real or complex number, x itself is returned.

Example

`y=prod(linspace(1,3,10))` returns 583.

See also

`sum()`, `avg()`, `max()`, `min()`

sum()

Sum of vector elements.

Syntax

y=sum(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function returns the sum of the elements of a real or complex vector.

For $x \in \mathbb{C}^n$: $y = \sum_{i=1}^n x_i$

For x being a real or complex number, x itself is returned.

Example

y=sum(linspace(1,3,10)) returns 20.

See also

prod(), avg(), max(), min()

xvalue()

Returns x -value which is associated with the y -value nearest to a specified y -value in a given vector.

Syntax

`x=xvalue(f,yval)`

Arguments

| Name | Type | Def. Range | Required |
|-------------------|------------------------------|-----------------------|--------------|
| <code>f</code> | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |
| <code>yval</code> | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the x -value which is associated with the y -value nearest to *yval* in the given vector *f*; therefore the vector *f* must have a single data dependency.

Example

`x=xvalue(f,1).`

See also

`yvalue()`, `interpolate()`

yvalue()

Returns y-value of a given vector which is located nearest to the specified x-value.

Syntax

`y=yvalue(f,xval)`

Arguments

| Name | Type | Def. Range | Required |
|------|------------------------------|-----------------------|----------|
| f | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |
| xval | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | ✓ |

Description

This function returns the y-value of the given vector f which is located nearest to the x-value $xval$; therefore the vector f must have a single data dependency.

Example

`y=yvalue(f,1).`

See also

`xvalue()`, `interpolate()`

Differentiation and Integration

ddx()

Differentiate mathematical expression with respect to a given variable.

Syntax

```
y=ddx(f(x),x)
```

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|----------------------|----------|---------|
| f(x) | | | ✓ | |
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^m, \mathbb{C}^m$ | $]-\infty, +\infty[$ | ✓ | |

Description

This function executes a symbolic differentiation on a function $f(x)$ with respect to a variable x . The result is evaluated at the contents x_0 of x .

$$y = \left. \frac{df}{dx} \right|_{x_0}$$

If x is a vector, the differential quotient is evaluated for all components of x , giving a result vector y .

Example

Create a vector x by setting `x=linspace(0,2,3)`, thus $x = [0, 1, 2]^T$. Entering

```
y=ddx(sin(x),x
```

 returns 1, 0.54, -0.416.

Why? $\frac{df}{dx} = \frac{d \sin(x)}{dx} = \cos(x)$, and $\cos(x)$ evaluated at $x = [0, 1, 2]^T$ gives the result above.

See also

`diff()`

diff()

Differentiate vector with respect to another vector.

Syntax

`z=diff(y,x,n)`

Arguments

| Name | Type | Def. Range | Required | Default |
|------|------------------------------|-----------------------|----------|---------|
| y | $\mathbb{R}^k, \mathbb{C}^k$ | $] -\infty, +\infty[$ | ✓ | |
| x | $\mathbb{R}^m, \mathbb{C}^m$ | $] -\infty, +\infty[$ | ✓ | |
| n | \mathbb{N} | | | 1 |

Description

This function numerically differentiates a vector y with respect to a vector x . If the optional integer parameter n is given, the n -th derivative is calculated. Differentiation is executed for $N=\min(k,m)$ elements. For $n=1$,

$$\frac{\Delta y_i}{\Delta x_i} = \begin{cases} \frac{1}{2} \left(\frac{y_i - y_{i-1}}{x_i - x_{i-1}} + \frac{y_{i+1} - y_i}{x_{i+1} - x_i} \right) & \text{for } N-1 > i > 0 \\ \frac{y_{i+1} - y_i}{x_{i+1} - x_i} & \text{for } i = 0 \\ \frac{y_i - y_{i-1}}{x_i - x_{i-1}} & \text{for } i = N-1 \end{cases}$$

If $n > 1$, the result of the differentiation above is assigned to y and the aforementioned differentiation step is repeated until the number of those steps is equal to n .

Example

`z=diff(linspace(1,3,3),linspace(2,3,3))` returns 2, 2, 2.

See also

`integrate()`, `sum()`, `max()`, `min()`

integrate()

Integrate vector.

Syntax

`z=integrate(y,h)`

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| y | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |
| h | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | \checkmark |

Description

This function numerically integrates a vector x with respect to a differential h . The integration method is according to the trapezoidal rule:

$$\int f(t) dt \approx h \left(\frac{y_0}{2} + y_1 + y_2 + \dots + y_{n-1} + \frac{y_n}{2} \right)$$

Example

Calculate an approximation of the integral $\int_1^3 t dt$ using 101 points:

`z=integrate(linspace(1,3,101))` returns 4.

See also

`diff()`, `sum()`, `max()`, `min()`

Signal Processing

dft()

Discrete Fourier Transform.

Syntax

`y=dft(v)`

Arguments

| Name | Type | Def. Range | Required |
|----------------|------------------------------|----------------------|--------------|
| <code>v</code> | $\mathbb{R}^n, \mathbb{C}^n$ | $]-\infty, +\infty[$ | \checkmark |

Description

This function computes the Discrete Fourier Transform (DFT) of a vector v . The advantage of this function compared to `fft()` is that the number n of components of v is arbitrary, while for the latter n must be a power of 2. The drawbacks are that `dft()` is slower and less accurate than `fft()`.

Example

This calculates the spectrum y of a DC signal:

| | |
|---|---------------------|
| <code>y=dft(linspace(1,1,7))</code> returns | <code>y</code> |
| | 1 |
| | -1.59e-17+j1.59e-17 |
| | \vdots |
| | 2.22e-16-j1.11e-16 |

Please note that in this example 7 points are used for the time vector v . Since 7 is not a power of 2, the same expression used together with the `fft()` function would lead to wrong results. Note also the rounding errors where “0” would be the correct value.

See also

`idft()`, `fft()`, `ifft()`, `Freq2Time()`, `Time2Freq()`

fft()

Fast Fourier Transform.

Syntax

`y=fft(v)`

Arguments

| Name | Type | Def. Range | Required |
|----------------|------------------------------|-----------------------|--------------|
| <code>v</code> | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function computes the Fast Fourier Transform (FFT) of a vector v . The number n of components of v must be a power of 2.

Example

This calculates the spectrum y of a DC signal:

`y=fft(linspace(1,1,8))` returns

| |
|----------------|
| <code>y</code> |
| 1 |
| 0 |
| \vdots |
| 0 |

See also

`ifft()`, `dft()`, `idft()`, `Freq2Time()`, `Time2Freq()`, `fftshift()`

idft()

Inverse Discrete Fourier Transform.

Syntax

`y=idft(v)`

Arguments

| Name | Type | Def. Range | Required |
|----------------|------------------------------|-----------------------|----------|
| <code>v</code> | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function computes the Inverse Discrete Fourier Transform (IDFT) of a vector v . The advantage of this function compared to `ifft()` is that the number n of components of v is arbitrary, while for the latter n must be a power of 2. The drawbacks are that `idft()` is slower and less accurate than `ifft()`.

Example

This calculates the time function y belonging to a white spectrum:

| | |
|--|---------------------|
| <code>y=idft(linspace(1,1,7))</code> returns | <code>y</code> |
| | 7 |
| | -1.11e-16-j1.11e-16 |
| | ⋮ |
| | 1.55e-15+j7.77e-16 |

Please note that in this example 7 points are used for the spectrum vector v . Since 7 is not a power of 2, the same expression used together with the `ifft()` function would lead to wrong results. Note also the rounding errors where “0” would be the correct value.

See also

dft(), ifft(), fft(), Freq2Time(), Time2Freq(), fftshift()

ifft()

Inverse Fast Fourier Transform.

Syntax

`y=ifft(v)`

Arguments

| Name | Type | Def. Range | Required |
|----------------|------------------------------|-----------------------|--------------|
| <code>v</code> | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function computes the Inverse Fast Fourier Transform (IFFT) of a vector v . The number n of components of v must be a power of 2.

Example

This calculates the time function y belonging to a white spectrum:

| | |
|--|----------------|
| <code>y=ifft(linspace(1,1,8))</code> returns | <code>y</code> |
| | 8 |
| | 0 |
| | \vdots |
| | 0 |

See also

`fft()`, `dft()`, `idft()`, `Freq2Time()`, `Time2Freq()`, `fftshift()`

fftshift()

Move the frequency 0 to the center of the FFT vector.

Syntax

$y = \text{fftshift}(v)$

Arguments

| Name | Type | Def. Range | Required |
|------|------------------------------|----------------------|--------------|
| v | $\mathbb{R}^n, \mathbb{C}^n$ | $]-\infty, +\infty[$ | \checkmark |

Description

This function shuffles the FFT values of vector v in order to move the frequency 0 to the center of the vector. Below of it the components with negative frequencies are located, above those with positive frequencies. Herewith the "classical" look of a spectrum as gained by a spectrum analyzer is obtained.

Example

Suppose x to be the result of a FFT of 8 elements, e.g.

| |
|----------|
| x |
| 1 |
| 2 |
| \vdots |
| 8 |

The result of the FFT is sorted in such a way that the component with frequency zero is the first element (1) of the vector. The components with positive frequency follow (2,3,4). After that, the components with negative frequency (5,6,7,8) are arranged, starting from the most negative value. This pattern can be exemplarily generated in Qucs by writing $x = \text{linspace}(1, 8, 8)$. Then

| |
|---|
| y |
| 5 |
| 6 |
| 7 |
| 8 |
| 1 |
| 2 |
| 3 |
| 4 |

y=fftshift(x) returns

As you can see, the component with frequency 0 (element 1) is moved to the middle of the spectrum vector. Beneath of it the components with negative frequencies appear (5,6,7,8), above those with positive frequencies (2,3,4).

See also

fft(), ifft(), dft(), idft()

Time2Freq()

Interpreted Discrete Fourier Transform.

Syntax

`y=Time2Freq(v,t)`

Arguments

| Name | Type | Def. Range | Required |
|----------------|------------------------------|-----------------------|--------------|
| <code>v</code> | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |
| <code>t</code> | $\mathbb{R}^k, \mathbb{C}^k$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function computes the Discrete Fourier Transform (DFT) of a vector v with respect to a time vector t .

Example

This calculates the spectrum $y(f)$ of a DC signal:

`y=Time2Freq(linspace(1,1,7),linspace(0,1,2))` returns

| Frequency | y |
|-----------|---------------------|
| 0 | 1 |
| 0.167 | -1.59e-17+j1.59e-17 |
| \vdots | \vdots |
| 1 | 2.22e-16-j1.11e-16 |

Please note that in this example 7 points are used for the time vector v . Note also the rounding errors at $t > 0$, where “0” would be the correct value.

See also

`idft()`, `fft()`, `ifft()`, `Freq2Time()`

Freq2Time()

Interpreted Inverse Discrete Fourier Transform.

Syntax

`y=Freq2Time(v,f)`

Arguments

| Name | Type | Def. Range | Required |
|------|------------------------------|-----------------------|----------|
| v | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |
| f | $\mathbb{R}^k, \mathbb{C}^k$ | $] -\infty, +\infty[$ | ✓ |

Description

This function computes the Inverse Discrete Fourier Transform (IDFT) of a vector v with respect to a frequency vector f .

Example

This calculates the time function $y(t)$ belonging to a white spectrum:

`y=Freq2Time(linspace(1,1,7),linspace(0,1,2))` returns

| Frequency | y |
|-----------|---------------------|
| 0 | 7 |
| 0.167 | -1.11e-16-j1.11e-16 |
| ⋮ | ⋮ |
| 1 | 1.55e-15+j7.77e-16 |

Please note that in this example 7 points are used for the spectrum vector v . Note also the rounding errors at $t > 0$, where “0” would be the correct value.

See also

`dft()`, `ifft()`, `fft()`, `Time2Freq()`

kbd()

Kaiser-Bessel derived window.

Syntax

y=kbd(a,n)

y=kbd(a)

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--------------|-----------------------|--------------|---------|
| a | \mathbb{R} | $] -\infty, +\infty[$ | \checkmark | |
| n | \mathbb{N} | $[1, +\infty[$ | | 64 |

Description

This function generates a Kaiser-Bessel window according to

$$y_k = \frac{\sum_{i=0}^k I_0 \left(\pi a \sqrt{1 - \left(\frac{4i}{n} - 1 \right)} \right)}{\sum_{i=0}^{\frac{n}{2}} I_0 \left(\pi a \sqrt{1 - \left(\frac{4i}{n} - 1 \right)} \right)},$$

$$y_{n-k-1} = y_k$$

for $0 \leq k < \frac{n}{2}$

If the parameter n is not specified, $n=64$ is assumed.

Example

y=kbd(0.1,4) returns .

See also

dft(), ifft(), fft()

Electronics Functions

Unit Conversion

dB()

dB value.

Syntax

y=dB(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the dB value of a real or complex number or vector.

$$y = 20 \log |x|$$

For x being a vector the equation above is applied to the components of x .

Example

y=db(10) returns 20.

See also

`log10()`

dbm()

Convert voltage to power in dBm.

Syntax

$y = \text{dBm}(u, Z0)$

$y = \text{dBm}(u)$

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|--------------|---------|
| u | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark | |
| $Z0$ | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | | 50 |

Description

This function returns the corresponding dBm power of a real or complex voltage or vector u . The impedance $Z0$ referred to is either specified or 50Ω .

$$y = 10 \log \frac{|u|^2}{Z_0 0.001W}$$

For u being a vector the equation above is applied to the components of u .

Please note that u is considered as a rms value, not as an amplitude.

Example

$y = \text{dbm}(1)$ returns 13.

See also

$\text{dbm2w}()$, $\text{w2dbm}()$, $\text{log10}()$

dbm2w()

Convert power in dBm to power in Watts.

Syntax

$y = \text{dBm2w}(x)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function converts the real or complex power or power vector, given in dBm, to the corresponding power in Watts.

$$y = 0.001 \cdot 10^{\frac{x}{10}}$$

For x being a vector the equation above is applied to the components of x .

Example

$y = \text{dbm2w}(10)$ returns 0.01.

See also

[dbm\(\)](#), [w2dbm\(\)](#)

w2dbm()

Convert power in Watts to power in dBm.

Syntax

y=w2dBm(x)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| x | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function converts the real or complex power or power vector, given in Watts, to the corresponding power in dBm.

$$y = 10 \log \frac{x}{0.001W}$$

For x being a vector the equation above is applied to the components of x .

Example

y=w2dbm(1) returns 30.

See also

dbm(), dbm2w(), log10()

Reflection Coefficients and VSWR

rtoswr()

Converts reflection coefficient to voltage standing wave ratio (VSWR).

Syntax

`s=rtoswr(r)`

Arguments

| Name | Type | Def. Range | Required |
|----------------|--|--------------|--------------|
| <code>r</code> | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $ r \leq 1$ | \checkmark |

Description

For a real or complex reflection coefficient r , this function calculates the corresponding voltage standing wave ratio (VSWR) s according to

$$s = \frac{1 + |r|}{1 - |r|}$$

VSWR is a real number and is usually given in the notation “s : 1”.

For r being a vector the equation above is applied to the components of r .

Examples

`s=rtoswr(0)` returns 1.

`s=rtoswr(0.1+0.2*i)` returns 1.58.

See also

`ytor()`, `ztor()`, `rtoy()`, `rtoz()`

rtoy()

Converts reflection coefficient to admittance.

Syntax

`y=rtoy(r)`

`y=rtoy(r, Z0)`

Arguments

| Name | Type | Def. Range | Required | Default |
|-----------------|--|-----------------------|--------------|---------|
| <code>r</code> | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $ r \leq 1$ | \checkmark | |
| <code>Z0</code> | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | | 50 |

Description

For a real or complex reflection coefficient r , this function calculates the corresponding admittance y according to

$$y = \frac{1}{Z_0} \frac{1-r}{1+r}$$

If the reference impedance $Z0$ is not provided, the function assumes $Z0 = 50\Omega$.

For r being a vector the equation above is applied to the components of r .

Example

`y=rtoy(0.333)` returns 0.01.

See also

`ytor()`, `ztor()`, `rtoswr()`

rtoz()

Converts reflection coefficient to impedance.

Syntax

`z=rtoz(r)`

`z=rtoz(r, Z0)`

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|----------|---------|
| r | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $ r \leq 1$ | ✓ | |
| Z0 | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | | 50 |

Description

For a real or complex reflection coefficient r , this function calculates the corresponding impedance Z according to

$$Z = Z_0 \frac{1 - r}{1 + r}$$

If the reference impedance $Z0$ is not provided, the function assumes $Z0 = 50\Omega$.

For r being a vector the equation above is applied to the components of r .

Example

`z=rtoz(0.333)` returns 99.9.

See also

`ztor()`, `ytor()`, `rtoswr()`

ytor()

Converts admittance to reflection coefficient.

Syntax

`r=ytor(Y)`

`r=ytor(Y, Z0)`

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|--------------|---------|
| Y | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark | |
| Z0 | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | | 50 |

Description

For a real or complex admittance y , this function calculates the corresponding reflection coefficient according to

$$r = \frac{1 - Y Z_0}{1 + Y Z_0}$$

For Y being a vector the equation above is applied to the components of Y .

If the reference impedance $Z0$ is not provided, the function assumes $Z0 = 50\Omega$.

Often a dB measure is given for the reflection coefficient, the so called “return loss”:

$$RL = -20 \log |r| \text{ [dB]}$$

Example

`r=ytor(0.01)` returns 0.333.

See also

`rtoz()`, `rtoz()`, `rtoswr()`, `log10()`, `dB()`

ztor()

Converts impedance to reflection coefficient.

Syntax

`r=ztor(Z)`

`r=ztor(Z, Z0)`

Arguments

| Name | Type | Def. Range | Required | Default |
|-----------------|--|-----------------------|--------------|---------|
| <code>Z</code> | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | \checkmark | |
| <code>Z0</code> | \mathbb{R}, \mathbb{C} | $] -\infty, +\infty[$ | | 50 |

Description

For a real or complex impedance Z , this function calculates the corresponding reflection coefficient according to

$$r = \frac{Z - Z_0}{Z + Z_0}$$

For Z being a vector the equation above is applied to the components of Z .

If the reference impedance $Z0$ is not provided, the function assumes $Z0 = 50\Omega$.

Often a dB measure is given for the reflection coefficient, the so called “return loss”:

$$RL = -20 \log |r| \text{ [dB]}$$

Example

`r=ztor(100)` returns 0.333.

See also

`rtoz()`, `rtoy()`, `rtoswr()`, `log10()`, `dB()`

N-Port Matrix Conversions

stos()

Converts S-parameter matrix to S-parameter matrix with different reference impedance(s).

Syntax

y=stos(S, Zref)

y=stos(S, Zref, Z0)

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|---|----------|---------|
| S | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}$ | $ S_{ij} \in]-\infty, +\infty[, 1 \leq i, j \leq n$ $ S_{ii} \leq 1, 1 \leq i \leq n$ | ✓ | |
| Zref | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ | |
| Z0 | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | | 50 |

Description

This function converts a real or complex scattering parameter matrix S into a scattering matrix Y . S has a reference impedance $Zref$, whereas the created scattering matrix Y has a reference impedance $Z0$.

If the reference impedance $Z0$ is not provided, the function assumes $Z0 = 50\Omega$.

Both $Zref$ and $Z0$ can be real or complex numbers or vectors; in the latter case the function operates on the elements of $Zref$ and $Z0$.

Example

Conversion of 50Ω terminated S-parameters to 100Ω terminated S-parameters:

`S2=stos(eye(2)*0.1,50,100)` returns

| | |
|--------|--------|
| -0.241 | 0 |
| 0 | -0.241 |

.

See also

`twoport()`, `stoy()`, `stoz()`

stoy()

Converts S-parameter matrix to Y-parameter matrix.

Syntax

$Y = \text{stoy}(S)$

$Y = \text{stoy}(S, Z_{\text{ref}})$

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|---|----------|---------|
| S | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}$ | $ S_{ij} \in]-\infty, +\infty[, 1 \leq i, j \leq n$ $ S_{ii} \leq 1, 1 \leq i \leq n$ | ✓ | |
| Zref | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | | 50 |

Description

This function converts a real or complex scattering parameter matrix S into an admittance matrix Y . S has a reference impedance Z_{ref} , which is assumed to be $Z_{\text{ref}} = 50\Omega$ if not provided by the user.

Z_{ref} can be real or complex number or vector; in the latter case the function operates on the elements of Z_{ref} .

Example

$Y = \text{stoy}(\text{eye}(2) * 0.1, 100)$ returns

| | |
|---------|---------|
| 0.00818 | 0 |
| 0 | 0.00818 |

.

See also

`twoport()`, `stos()`, `stoz()`, `ytoz()`

stoz()

Converts S-parameter matrix to Z-parameter matrix.

Syntax

$Z = \text{stoz}(S)$

$Z = \text{stoz}(S, Z_{\text{ref}})$

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|---|----------|---------|
| S | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}$ | $ S_{ij} \in]-\infty, +\infty[, 1 \leq i, j \leq n$ $ S_{ii} \leq 1, 1 \leq i \leq n$ | ✓ | |
| Zref | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | | 50 |

Description

This function converts a real or complex scattering parameter matrix S into an impedance matrix Z . S has a reference impedance Z_{ref} , which is assumed to be $Z_{\text{ref}} = 50\Omega$ if not provided by the user.

Z_{ref} can be real or complex number or vector; in the latter case the function operates on the elements of Z_{ref} .

Example

$Z = \text{stoz}(\text{eye}(2) * 0.1, 100)$ returns

| | |
|-----|-----|
| 122 | 0 |
| 0 | 122 |

.

See also

`twoport()`, `stos()`, `stoy()`, `ztos()`

twoport()

Converts a two-port matrix from one representation into another.

Syntax

U=twoport(X, from, to)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-------------------------------------|----------|
| X | $\mathbb{R}^{2 \times 2}, \mathbb{C}^{2 \times 2}$ | $]-\infty, +\infty[$ | ✓ |
| from | Character | {'Y', 'Z', 'H', 'G', 'A', 'S', 'T'} | ✓ |
| to | Character | {'Y', 'Z', 'H', 'G', 'A', 'S', 'T'} | ✓ |

Description

This function converts a real or complex two-port matrix X from one representation into another.

Example

Transfer a two-port Y matrix Y1 into a Z matrix:

Y1=eye(2)*0.1

Z1=twoport(Y1,'Y','Z') returns

| | |
|----|----|
| 10 | 0 |
| 0 | 10 |

.

See also

stos(), ytos(), ztos(), stoz(), stoy(), ytoz(), ztoy()

ytos()

Converts Y-parameter matrix to S-parameter matrix.

Syntax

$S = \text{ytos}(Y)$

$S = \text{ytos}(Y, Z0)$

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|----------|---------|
| Y | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}$ | $] -\infty, +\infty[$ | ✓ | |
| Z0 | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | | 50 |

Description

This function converts a real or complex admittance matrix Y into a scattering parameter matrix S . Y has a reference impedance $Z0$, which is assumed to be $Z0 = 50\Omega$ if not provided by the user.

$Z0$ can be real or complex number or vector; in the latter case the function operates on the elements of $Z0$.

Example

$S = \text{ytos}(\text{eye}(2) * 0.1, 100)$ returns

| | |
|--------|--------|
| -0.818 | 0 |
| 0 | -0.818 |

.

See also

`twoport()`, `stos()`, `ztos()`, `stoy()`

ytoz()

Converts Y-parameter matrix to Z-parameter matrix.

Syntax

$Z = \text{ytoz}(Y)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| Y | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function converts a real or complex admittance matrix Y into an impedance matrix Z .

Example

$Z = \text{ytoz}(\text{eye}(2) * 0.1)$ returns

| | |
|----|----|
| 10 | 0 |
| 0 | 10 |

.

See also

`twoport()`, `ztoy()`

ztos()

Converts **Z**-parameter matrix to **S**-parameter matrix.

Syntax

$S = \text{ztos}(Z)$

$S = \text{ztos}(Z, Z0)$

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|--------------|---------|
| Z | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}$ | $] -\infty, +\infty[$ | \checkmark | |
| $Z0$ | $\mathbb{R}, \mathbb{C}, \mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | | 50 |

Description

This function converts a real or complex impedance matrix Z into a scattering parameter matrix S . Z has a reference impedance $Z0$, which is assumed to be $Z0 = 50\Omega$ if not provided by the user.

$Z0$ can be real or complex number or vector; in the latter case the function operates on the elements of $Z0$.

Example

$S = \text{ztos}(\text{eye}(2) * 0.1, 100)$ returns

| | |
|--------|--------|
| -0.998 | 0 |
| 0 | -0.998 |

.

See also

`twoport()`, `twoport()`, `stos()`, `ytos()`, `stoz()`

ztoy()

Converts Z-parameter matrix to Y-parameter matrix.

Syntax

$Y = \text{ztoy}(Z)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|----------------------|--------------|
| Z | $\mathbb{R}^{n \times n}, \mathbb{C}^{n \times n}$ | $]-\infty, +\infty[$ | \checkmark |

Description

This function converts a real or complex impedance matrix Z into an admittance matrix Y .

Example

$Y = \text{ztoy}(\text{eye}(2) * 0.1)$ returns

| | |
|----|----|
| 10 | 0 |
| 0 | 10 |

.

See also

`twoport()`, `ytoz()`

Amplifiers

GaCircle()

Circle(s) with constant available power gain Ga in the source plane.

Syntax

y=GaCircle(X,Ga,v)

y=GaCircle(X,Ga,n)

y=GaCircle(X,Ga)

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|----------|---------|
| X | $\mathbb{R}^{2 \times 2 \times p}, \mathbb{C}^{2 \times 2 \times p}$ | $] -\infty, +\infty[$ | ✓ | |
| v | \mathbb{R}^n | $[0, 360]^o$ | | |
| Ga | \mathbb{R}, \mathbb{R}^m | $[0, +\infty[$ | ✓ | |
| n | N | $[2, +\infty[$ | | 64 |

Description

This function generates the points of the circle of constant available power gain G_A in the complex source plane (r_S) of an amplifier. The amplifier is described by a two-port S-parameter matrix S . Radius r and center c of this circle are calculated as follows:

$$r = \frac{\sqrt{1 - 2 \cdot K \cdot g_A \cdot |S_{12}S_{21}| + g_A^2 \cdot |S_{12}S_{21}|^2}}{|1 + g_A \cdot (|S_{11}|^2 - |\Delta|^2)|} \text{ and } c = \frac{g_A (S_{11}^* - S_{22} \Delta^*)}{1 + g_A (|S_{11}|^2 - |\Delta|^2)},$$

where $g_A = \frac{G_A}{|S_{21}|^2}$ and K Rollet stability factor. Δ denotes determinant of S .

The points of the circle can be specified by the angle vector v , where the angle must be given in degrees. Another possibility is to specify the number n of angular equally distributed points around the circle. If no additional argument to X is given, 64 points are taken. The available power gain can also be specified in a vector Ga , leading to the generation of m circles, where m is the size of Ga .

Please also refer to “Qucs - Technical Papers”, chapter 1.5.

Example

```
v=GaCircle(S)
```

See also

GpCircle(), Rollet()

GpCircle()

Circle(s) with constant operating power gain Gp in the load plane.

Syntax

y=GpCircle(X,Gp,v)

y=GpCircle(X,Gp,n)

y=GpCircle(X,Gp)

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|----------|---------|
| X | $\mathbb{R}^{2 \times 2 \times p}, \mathbb{C}^{2 \times 2 \times p}$ | $] -\infty, +\infty[$ | ✓ | |
| v | \mathbb{R}^n | $[0, 360]^o$ | | |
| Gp | \mathbb{R}, \mathbb{R}^m | $[0, +\infty[$ | ✓ | |
| n | \mathbb{N} | $[2, +\infty[$ | | 64 |

Description

This function generates the points of the circle of constant operating power gain G_P in the complex load plane (r_L) of an amplifier. The amplifier is described by a two-port S-parameter matrix S . Radius r and center c of this circle are calculated as follows:

$$r = \frac{\sqrt{1 - 2 \cdot K \cdot g_P \cdot |S_{12}S_{21}| + g_P^2 \cdot |S_{12}S_{21}|^2}}{|1 + g_P \cdot (|S_{22}|^2 - |\Delta|^2)|} \text{ and } c = \frac{g_A (S_{22}^* - S_{11} \Delta^*)}{1 + g_P (|S_{22}|^2 - |\Delta|^2)},$$

where $g_A = \frac{G_P}{|S_{21}|^2}$ and K Rollet stability factor. Δ denotes determinant of S .

The points of the circle can be specified by the angle vector v , where the angle must be given in degrees. Another possibility is to specify the number n of angular equally distributed points around the circle. If no additional argument to X is

given, 64 points are taken. The available power gain can also be specified in a vector G_p , leading to the generation of m circles, where m is the size of G_p .

Please also refer to “Qucs - Technical Papers”, chapter 1.5.

Example

```
v=GpCircle(S)
```

See also

GaCircle(), Rollet()

Mu()

Mu stability factor of a two-port S-parameter matrix.

Syntax

y=Mu(S)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| S | $\mathbb{R}^{2 \times 2 \times p}, \mathbb{C}^{2 \times 2 \times p}, \mathbb{R}^{2 \times 2}, \mathbb{C}^{2 \times 2}$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the Mu stability factor μ of an amplifier being described by a two-port S-parameter matrix S :

$$\mu = \frac{1 - |S_{11}|^2}{|S_{22} - S_{11}^* \Delta| + |S_{21} S_{12}|}$$

Δ denotes determinant of S .

The amplifier is unconditionally stable if $\mu > 1$.

For S being a vector of matrices the equation above is applied to the sub-matrices of S .

Example

m=Mu(S)

See also

Mu2(), Rollet(), StabCircleS(), StabCircleL()

Mu2()

Mu' stability factor of a two-port S-parameter matrix.

Syntax

y=Mu2(S)

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|--------------|
| S | $\mathbb{R}^{2 \times 2 \times p}, \mathbb{C}^{2 \times 2 \times p}, \mathbb{R}^{2 \times 2}, \mathbb{C}^{2 \times 2}$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the Mu' stability factor μ' of an amplifier being described by a two-port S-parameter matrix S :

$$\mu' = \frac{1 - |S_{22}|^2}{|S_{11} - S_{22}^* \Delta| + |S_{21} S_{12}|}$$

Δ denotes determinant of S .

The amplifier is unconditionally stable if $\mu' > 1$.

For S being a vector of matrices the equation above is applied to the sub-matrices of S .

Example

m=Mu2(S)

See also

Mu2(), Rollet(), StabCircleS(), StabCircleL()

NoiseCircle()

Generates circle(s) with constant Noise Figure(s).

Syntax

y=NoiseCircle(Sopt,Fmin,Rn,F,v)

y=NoiseCircle(Sopt,Fmin,Rn,F,n)

y=NoiseCircle(Sopt,Fmin,Rn,F)

Arguments

| Name | Type | Def. Range | Required | Default |
|------|------------------------------|----------------------|----------|---------|
| Sopt | $\mathbb{R}^n, \mathbb{C}^n$ | $]-\infty, +\infty[$ | ✓ | |
| Fmin | \mathbb{R}^n | $[1, +\infty[$ | ✓ | |
| Rn | $\mathbb{R}^n, \mathbb{C}^n$ | $[0, +\infty[$ | ✓ | |
| F | \mathbb{R}, \mathbb{R}^n | $[1, +\infty[$ | ✓ | |
| v | \mathbb{R}^n | $[0, 360]^o$ | | |
| n | \mathbb{N} | $[2, +\infty[$ | | 64 |

Description

This function generates the points of the circle of constant Noise Figure (NF) F in the complex source plane (r_S) of an amplifier. Generally, the amplifier has its minimum NF F_{min} , if the source reflection coefficient $r_S = S_{opt}$ (noise matching). Note that this state with optimum source reflection coefficient S_{opt} is different from power matching ! Thus power gain under noise matching is lower than the maximum obtainable gain. The values of S_{opt} , F_{min} and the normalised equivalent noise resistance R_n/Z_0 can be usually taken from the data sheet of the amplifier.

Radius r and center c of the circle of constant NF are calculated as follows:

$$r = \frac{\sqrt{N^2 + N \cdot (1 - |S_{opt}|^2)}}{1 + N} \text{ and } c = \frac{S_{opt}}{1 + N}, \text{ with } N = \frac{F - F_{min}}{4 R_n} \cdot Z_0 \cdot |1 + S_{opt}|^2$$

The points of the circle can be specified by the angle vector v , where the angle must be given in degrees. Another possibility is to specify the number n of angular equally distributed points around the circle. If no additional argument to X is given, 64 points are taken.

Please also refer to “Qucs - Technical Papers”, chapter 2.2.

Example

```
v=NoiseCircle(Sopt,Fmin,Rn,F)
```

See also

GaCircle(), GpCircle()

PlotVs()

Returns a data item based upon vector or matrix vector with dependency on a given vector.

Syntax

$y = \text{PlotVs}(X, v)$

Arguments

| Name | Type | Def. Range | Required |
|------|--|-----------------------|----------|
| X | $\mathbb{R}^n, \mathbb{C}^n, \mathbb{R}^{m \times n \times p}, \mathbb{C}^{m \times n \times p}$ | $] -\infty, +\infty[$ | ✓ |
| v | $\mathbb{R}^n, \mathbb{C}^n$ | $] -\infty, +\infty[$ | ✓ |

Description

This function returns a data item based upon a vector or matrix vector X with dependency on a given vector v .

Example

$\text{PlotVs}(\text{Gain}, \text{frequency}/1\text{E9}).$

See also

Rollet()

Rollet stability factor of a two-port S-parameter matrix.

Syntax

y=Rollet(S)

Arguments

| Name | Type | Def. Range | Required |
|------|---|-----------------------|--------------|
| S | $\mathbb{R}^{2 \times 2 \times p}$, $\mathbb{C}^{2 \times 2 \times p}$, $\mathbb{R}^{2 \times 2}$, $\mathbb{C}^{2 \times 2}$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the Rollet stability factor K of an amplifier being described by a two-port S-parameter matrix S :

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2 |S_{21}| |S_{12}|}$$

Δ denotes determinant of S .

The amplifier is unconditionally stable if $K > 1$ and $|\Delta| < 1$.

Note that a large K may be misleading in case of a multi-stage amplifier, pretending extraordinary stability. This is in conflict with reality where a large gain amplifier usually suffers from instability due to parasitics.

For S being a vector of matrices the equation above is applied to the sub-matrices of S .

Example

K=Rollet(S)

See also

Mu(), Mu2(), StabCircleS(), StabCircleL()

StabCircleL()

Stability circle in the load plane.

Syntax

y=StabCircleL(X)

y=StabCircleL(X,v)

y=StabCircleL(X,n)

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|--------------|---------|
| X | $\mathbb{R}^{2 \times 2 \times p}, \mathbb{C}^{2 \times 2 \times p}$ | $] -\infty, +\infty[$ | \checkmark | |
| v | \mathbb{R}^n | $[0, 360]^o$ | | |
| n | \mathbb{N} | $[2, +\infty[$ | | 64 |

Description

This function generates the stability circle points in the complex load reflection coefficient (r_L) plane of an amplifier. The amplifier is described by a two-port S-parameter matrix S . Radius r and center c of this circle are calculated as follows:

$$r = \left| \frac{S_{21} S_{12}}{|S_{22}|^2 - |\Delta|^2} \right| \text{ and } c = \frac{S_{22}^* - S_{11} \cdot \Delta^*}{|S_{22}|^2 - |\Delta|^2}$$

Δ denotes determinant of S .

The points of the circle can be specified by the angle vector v , where the angle must be given in degrees. Another possibility is to specify the number n of angular equally distributed points around the circle. If no additional argument to X is given, 64 points are taken.

If the center of the r_L plane lies within this circle and $|S_{11}| \leq 1$ then the circuit is stable for all reflection coefficients inside the circle. If the center of the r_L plane lies outside the circle and $|S_{11}| \leq 1$ then the circuit is stable for all reflection coefficients outside the circle (please also refer to “Qucs - Technical Papers”, chapter 1.5).

Example

`v=StabCircleL(S)`

See also

`StabCircleS()`, `Rollet()`, `Mu()`, `Mu2()`

StabCircleS()

Stability circle in the source plane.

Syntax

y=StabCircleS(X)

y=StabCircleS(X,v)

y=StabCircleS(X,n)

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--|-----------------------|--------------|---------|
| X | $\mathbb{R}^{2 \times 2 \times p}, \mathbb{C}^{2 \times 2 \times p}$ | $] -\infty, +\infty[$ | \checkmark | |
| v | \mathbb{R}^n | $[0, 360]^o$ | | |
| n | \mathbb{N} | $[2, +\infty[$ | | 64 |

Description

This function generates the stability circle points in the complex source reflection coefficient (r_S) plane of an amplifier. The amplifier is described by a two-port S-parameter matrix S . Radius r and center c of this circle are calculated as follows:

$$r = \left| \frac{S_{21} S_{12}}{|S_{11}|^2 - |\Delta|^2} \right| \text{ and } c = \frac{S_{11}^* - S_{22} \cdot \Delta^*}{|S_{11}|^2 - |\Delta|^2}$$

Δ denotes determinant of S .

The points of the circle can be specified by the angle vector v , where the angle must be given in degrees. Another possibility is to specify the number n of angular equally distributed points around the circle. If no additional argument to X is given, 64 points are taken.

If the center of the r_S plane lies within this circle and $|S_{22}| \leq 1$ then the circuit is stable for all reflection coefficients inside the circle. If the center of the r_S plane lies outside the circle and $|S_{22}| \leq 1$ then the circuit is stable for all reflection coefficients outside the circle (please also refer to “Qucs - Technical Papers”, chapter 1.5).

Example

`v=StabCircleS(S)`

See also

`StabCircleL()`, `Rollet()`, `Mu()`, `Mu2()`

StabFactor()

Stability factor of a two-port S-parameter matrix. Synonym for Rollet()

Syntax

```
y=StabFactor(S)
```

See also

Rollet()

StabMeasure()

Stability measure **B1** of a two-port **S**-parameter matrix.

Syntax

y=StabMeasure(S)

Arguments

| Name | Type | Def. Range | Required |
|------|---|-----------------------|--------------|
| S | $\mathbb{R}^{2 \times 2 \times p}$, $\mathbb{C}^{2 \times 2 \times p}$, $\mathbb{R}^{2 \times 2}$, $\mathbb{C}^{2 \times 2}$ | $] -\infty, +\infty[$ | \checkmark |

Description

This function returns the stability measure *B1* of a two-port S-parameter matrix *S*:

$$B1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2$$

Δ denotes determinant of *S*.

The amplifier is unconditionally stable if *B1* > 0 and the Rollet factor *K* > 1.

For *S* being a vector of matrices the equation above is applied to the sub-matrices of *S*.

Example

B1=StabMeasure(S)

See also

Rollet(), Mu(), Mu2(), StabCircleS(), StabCircleL()

vt()

Thermal voltage for a given temperature in Kelvin.

Syntax

y=vt(t)

Arguments

| Name | Type | Def. Range | Required | Default |
|------|--------------|----------------|--------------|---------|
| t | \mathbb{R} | $[0, +\infty[$ | \checkmark | |

Description

This function returns the corresponding thermal voltage V_t in Volt of a real absolute temperature (vector) T in Kelvin according to

$$V_t = \frac{kT}{e}$$

where k is the Boltzmann constant and e denotes the electrical charge on the electron. For t being a vector the equation above is applied to the components of k .

Please note that t is always larger than or equal to zero.

Example

y=vt(300) returns 0.0259.

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